

# GROUND STATE AND SADDLE POINT: MASSES AND DEFORMATIONS FOR EVEN-EVEN SUPERHEAVY NUCLEI WITH $98 \leq Z \leq 126$ AND $134 \leq N \leq 192$

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## Abstract

We determine ground-state and saddle-point shapes and masses of even-even superheavy nuclei in the range of proton numbers  $98 \leq Z \leq 126$  and neutron numbers  $134 \leq N \leq 192$ . Our study is performed within the microscopic-macroscopic method. The Strutinsky shell and pairing correction is calculated for the deformed Woods-Saxon single-particle potential and the Yukawa-plus-exponential energy is taken as a smooth part. We use parameters of the model that were fitted previously to this region of nuclei. A high-dimensional deformation space, including nonaxial and reflection-asymmetric shapes, is used in the search for saddle points. Both ground-state and saddle-point shapes are found with the aid of the minimization procedure, with dynamical programming technique of search for saddle points. The results are collected in two tables. Calculated ground-state mass-excess,  $Q_\alpha$  energies, total and macroscopic energies normalized to the macroscopic energy at the spherical shape, shell corrections (including pairing) and deformations are given for each nucleus in the table one. The second table gives the same properties, but at the saddle-point configuration. The obtained results are discussed and compared with available experimental data for alpha-decay energies ( $Q_\alpha$ ) and ground-state masses.

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## 1. Introduction

The uncharted region of the  $Z$ - $N$  plane can answer many questions of fundamental importance for science: How many neutrons can be bound in a nucleus? What are the unique properties of short-lived nuclei having extreme values of  $N/Z$ ? What are the properties of effective nuclear interactions in the environment different from that in stable nuclei? There is also an unsettled question of what can be the largest possible atomic number  $Z$  of an atomic nucleus. The recent experiments in Dubna claim the existence of a  $Z = 114, 115, 116, 117, 118$  system [1–11], with confirmation of hot fusion cross-sections coming from GSI [12] and LBL Berkeley [13]. For lighter elements:  $Z = 107, 108, 109, 110, 111, 112$  successful syntheses were done at the GSI laboratory [14–23].

The presented tables contain ground state (g.s.) and saddle point (s.p.) properties of even-even superheavy nuclei that were obtained within the microscopic-macroscopic method in a multidimensional deformation space. This conceptually

simple method is very convenient for determining many nuclear properties with relatively high accuracy, unattainable by other models, particularly in the area of heaviest elements. It makes possible global calculations of fission properties in this area of the atomic nuclei. Such systematic predictions relate to the questions specified above and contribute to a view on this exotic nuclear domain. At the same time, they can help in the interpretation of present experiments and inspire efforts towards new ones.

Atomic masses (binding energies) have been experimentally determined for nearly 2300 nuclei [24]. For almost 800 nuclei mass is measured more precisely than to 5 keV, for other 1000 nuclei - with the accuracy of 5-50 keV. The binding energy determines energy available for nuclear reactions and decays (and thus the creation of elements by stellar nucleosynthesis), and holds the key to the fundamental question of how the heavy elements came to existence. The best available theoretical global mass calculations predict the mass values with an approximate deviation 500-800 keV. Ground state masses calculated within the Hartree-Fock-Bogoliubov (HFB) method [25, 26] fitted to the fission data through adjustment of a vibrational term in the phenomenological collective correction have the r.m.s deviation equal 0.729 MeV. Macroscopic-microscopic global calculations of nuclear ground state masses made by P. Moller and co-workers [27] give the r.m.s error 0.669 MeV for nuclei ranging from Oxygen to Hassium and 0.448 MeV in the case of nuclei above  $N = 65$ . Phenomenological formula with the 10 free parameters given by Duflo and Zuker [28, 29] gives mass estimates with the 0.574 MeV r.m.s error. So, nuclear masses are presently measured at least ten times more precisely than they can be calculated.

Although theoretical predictions sometimes differ quantitatively, they consistently predict prolate deformed super-heavy nuclei with  $Z = 100-112$ , which is confirmed experimentally for nuclei around  $^{254}\text{No}$  [30], and spherical or oblate deformed systems with  $Z = 114$  and  $N = 174-184$  [31–36]. There are relatively many published predictions of the ground state properties of heaviest elements [25–29, 37]. Much rarer are analogous calculations at the saddle points, although they are necessary to estimate the cross sections (survival probabilities) for the synthesis of SHN [38]. This work provides the necessary theoretical saddle point data.

As the principle of the macroscopic -microscopic method is well known, only a brief description of it is given in Sect. 2, specifying involved quantities, their computation and the adopted values of parameters. In Sect. 3 we describe a variety of considered nuclear shapes which is an important ingredient of the model. The method for saddle point search is described in section 4, numerical tests applied to certify the results are mentioned in Sect. 5. Results and discussion are given in Sect. 6, a short summary in Sect. 7.

## 2. Method

The total nuclear binding energy ( $E$ ), which depends on the proton number  $Z$ , and neutron number  $N$  and the nuclear shape, can be written as a sum of a macroscopic ( $E_{mac}$ ) and a microscopic ( $E_{mic}$ ) energy:

$$E(def, Z, N) = E_{mic}(def, Z, N) + E_{mac}(def, Z, N). \quad (1)$$

### 2.1. Macroscopic energy

The macroscopic part of atomic mass is a sum of masses of atomic constituents and the macroscopic energy. As  $E_{mac}$ , it is a smooth function of proton and neutron number. In our analysis, it is taken in the liquid-drop form [41, 42]:

$$\begin{aligned}
M_{\text{macr}}(Z, N, \beta_\lambda^0) &= M_{\text{H}}Z + M_{\text{n}}N - a_{\text{v}}(1 - \kappa_{\text{v}}I^2)A + a_{\text{s}}(1 - \kappa_{\text{s}}I^2)A^{2/3}B_{\text{S}}(\{\beta_\lambda^0\}) \\
&+ a_0A^0 + c_1Z^2A^{-1/3}B_{\text{C}}(\{\beta_\lambda^0\}) - c_4Z^{4/3}A^{-1/3} \\
&+ f(k_{\text{F}}r_{\text{p}})Z^2A^{-1} - c_{\text{a}}(N - Z) - a_{\text{el}}Z^{2.39},
\end{aligned} \tag{2}$$

where  $M_{\text{H}}$  is mass of the hydrogen atom,  $M_{\text{n}}$  is mass of neutron,  $I = (N - Z)/A$  is the relative neutron excess,  $A = Z + N$  is the mass number of a nucleus. The functions  $B_{\text{S}}(\beta_\lambda)$  and  $B_{\text{C}}(\beta_\lambda)$  describe the dependence of the surface and Coulomb energies, respectively, on deformations  $\beta_\lambda$ , and  $\beta_\lambda^0$  are the values of these deformations at equilibrium. We adopted these functions in the form given by the Yukawa-plus-exponential model formulated by Krappe and Nix [41]. They read [27, 43]:

$$B_{\text{S}} = \frac{A^{-2/3}}{8\pi^2 r_0^2 a^4} \int \int_V \left(2 - \frac{r_{12}}{a}\right) \frac{e^{-r_{12}/a}}{r_{12}/a} d^3r_1 d^3r_2, \tag{3}$$

$$B_{\text{C}} = \frac{15}{32\pi^2} \frac{A^{-5/3}}{r_0^5} \int \int_V \frac{1}{r_{12}} \left[1 - \left(1 + \frac{1}{2} \frac{r_{12}}{a_{\text{den}}}\right) e^{-r_{12}/a_{\text{den}}}\right] d^3r_1 d^3r_2, \tag{4}$$

where  $r_{12} = |\vec{r}_1 - \vec{r}_2|$  with  $\vec{r}_1$  and  $\vec{r}_2$  describing the positions of two interacting volume elements,  $a$  is the range of the Yukawa interaction on which the model is based,  $a_{\text{den}}$  is the range of the Yukawa function used to generate nuclear charge distribution. The functions are normalized in such a way that they are equal 1 for a spherical nucleus in the limit case of  $a=0$  (for  $B_{\text{S}}$ ) and  $a_{\text{den}}=0$  (for  $B_{\text{C}}$ ), corresponding to the traditional liquid-drop model with a sharp surface. The integrations are over the volume of a nucleus. After turning them into surface integrals,  $B_{\text{S}}$  and  $B_{\text{C}}$  were calculated by using a four-fold (or three-fold, for axial symmetry) 64-point Gaussian quadrature.

The quantities  $c_1$  and  $c_4$  appearing in the Coulomb energy and the Coulomb exchange correction, respectively, are

$$c_1 = \frac{3}{5} \frac{e^2}{r_0}, \quad c_4 = \frac{5}{4} \left(\frac{3}{2\pi}\right)^{2/3} c_1, \tag{5}$$

where  $e$  is the elementary electric charge and  $r_0$  is the nuclear-radius parameter. The quantity  $f(k_{\text{F}}r_{\text{p}})$  appearing in the proton form-factor correction to the Coulomb energy in Eq. (2) has the form

$$f(k_{\text{F}}r_{\text{p}}) = -\frac{1}{8} \frac{e^2 r_{\text{p}}^2}{r_0^3} \left[ \frac{145}{48} - \frac{327}{2880} (k_{\text{F}}r_{\text{p}})^2 + \frac{1527}{1\,209\,600} (k_{\text{F}}r_{\text{p}})^4 \right], \tag{6}$$

where the Fermi wave number is

$$k_{\text{F}} = \left(\frac{9\pi Z}{4A}\right)^{1/3} r_0^{-1}, \tag{7}$$

and  $r_{\text{p}}$  is the proton root-mean-square radius. The last term in Eq. (2) describes the binding energy of electrons and  $a_{\text{v}}$ ,  $\kappa_{\text{v}}$ ,  $a_{\text{s}}$ ,  $\kappa_{\text{s}}$ ,  $a_0$ ,  $c_{\text{a}}$  are adjustable parameters. Thus, only two of these parameters ( $a_{\text{s}}$  and  $\kappa_{\text{s}}$ ) appear at the term, which depends on deformation. The four remaining parameters stand at the terms independent of the shape of a nucleus.

The macroscopic part of mass, Eq. (2), is used the same as in [42], except that three of its adjustable parameters:  $a_{\text{v}}$ ,  $\kappa_{\text{v}}$  and  $a_0$  were fitted to experimental masses of even-even heaviest nuclei with  $Z \geq 84$ . The result was

$$a_{\text{v}} = 16.0643, \quad \kappa_{\text{v}} = 1.9261, \quad a_0 = 17.926. \tag{8}$$

Following the authors of [42], we omit here the two terms considered in [43]: charge-asymmetry term  $c_{\text{a}}(N - Z)$  and Wigner term (characterized by a coefficient  $W$ ), as they do not significantly change the quality of the description of



masses of heaviest nuclei. The values of other parameters are adopted after [43]:

$$a_s = 21.13 \text{ MeV}, \quad \kappa_s = 2.30, \quad (9)$$

$$\begin{aligned} a &= 0.68 \text{ fm}, & a_{\text{den}} &= 0.70 \text{ fm}, & r_0 &= 1.16 \text{ fm}, \\ r_p &= 0.80 \text{ fm}, & a_{\text{el}} &= 1.433 \cdot 10^{-5} \text{ MeV}. \end{aligned} \quad (10)$$

## 2.2. Microscopic energy

The Strutinski shell correction [44, 45], based on the deformed Woods-Saxon single-particle potential, is taken for the microscopic part:

$$\begin{aligned} E_{\text{mic}}(def, Z, N) &= E_{\text{corr}}^{\text{sh}}(def, Z, N) \\ &+ E_{\text{corr}}^{\text{pair}}(def, Z, N), \end{aligned} \quad (11)$$

where  $E_{\text{corr}}^{\text{sh}}$  and  $E_{\text{corr}}^{\text{pair}}$  are the shell and pairing corrections, respectively.

### 2.2.1. Woods-Saxon potential

The Woods-Saxon potential  $V_{\text{WS}}$  has the following form:

$$V_{\text{WS}}(\vec{r}) = -\frac{V}{1 + e^{d(\vec{r}, \text{def})/a_{\text{ws}}}}, \quad (12)$$

where  $V$  is the depth of the potential,  $d(\vec{r}, \text{def})$  is the distance from the point  $\vec{r}$  to the surface of the nucleus,  $a_{\text{ws}}$  is the diffuseness of the nuclear surface. The symbol *def* stands for deformation which defines the nuclear surface (see Sect. 3). The depth of the potential is

$$V = V_0(1 \pm \kappa I), \quad (13)$$

where  $I = (N - Z)/A$  is the relative neutron excess and  $V_0$  and  $\kappa$  are adjustable parameters. The sign (+) is for protons and (−) for neutrons.

In the case of spherical shape, the potential is

$$V_{\text{WS}}(\vec{r}) = -\frac{V}{1 + e^{(r-R_0)/a_{\text{ws}}}}, \quad (14)$$

where  $R_0 = r_0 A^{1/3}$ .

The full microscopic potential has the form (e.g. [47]):

$$V_{\text{micr}} = V_{\text{WS}} + \lambda \left( \frac{\hbar}{2mc} \right)^2 \left( \frac{A}{A-1} \right)^2 (\nabla V_{\text{WS}}^{\text{s.o.}}) \cdot (\vec{\sigma} \times \vec{p}/\hbar) + V_c, \quad (15)$$

where the second term is the spin-orbit potential and the third term is the Coulomb potential, which has the following form:

$$V_c(\vec{r}) = \rho_c \int \frac{d^3 r'}{|\vec{r} - \vec{r}'|}, \quad (16)$$

where  $\rho_c = 3(Z-1)e/(4\pi R_0^3)$  is the uniform density and the integration extends over the volume enclosed by the nuclear surface.

Here we use the "universal" set of parameters of the potential given in [47]

$$\begin{aligned} r_0 &= 1.275 \text{ fm}, & (r_0)_{\text{so}} &= 1.32 \text{ fm}, & \lambda &= 36.0 \text{ for protons,} \\ r_0 &= 1.347 \text{ fm}, & (r_0)_{\text{so}} &= 1.31 \text{ fm}, & \lambda &= 35.0 \text{ for neutrons,} \\ V_0 &= 49.6 \text{ MeV}, & a_{\text{ws}} &= 0.70 \text{ fm}, & \kappa &= 0.86, \end{aligned}$$

where  $r_0$  and  $(r_0)_{\text{so}}$  are the radius parameters for the central and spin-orbit parts of the potential, respectively.

The single-particle potential is diagonalized in the deformed-oscillator basis. The  $n_p = 450$  lowest proton levels and  $n_n = 550$  lowest neutron levels from the  $N_{\text{max}} = 19$  lowest shells of the deformed harmonic oscillator are taken into account in the diagonalization procedure. We have determined the single - particle spectra for every investigated nucleus. These calculations therefore do not include any scaling relation to the *central* nucleus. A standard value of  $\hbar\omega_0 = 41/A^{1/3}$  MeV is taken for the oscillator energy.

### 2.2.2. Shell correction

The shell correction energy is calculated as proposed by Strutinski [44, 45]:

$$E_{\text{corr}}^{\text{sh}} = E_{\text{micro}} - \tilde{E}_{\text{micro}}, \quad (17)$$

where  $E_{\text{micro}}$  is the sum of single-particle energies over all occupied energy levels,

$$E_{\text{micro}} = \sum_{\nu_{\text{occ}}} \varepsilon_{\nu} = \int_{-\infty}^{\varepsilon_{\text{F}}} \rho(\varepsilon) \varepsilon d\varepsilon, \quad (18)$$

and

$$\rho(\varepsilon) = \sum_{\nu} \delta(\varepsilon - \varepsilon_{\nu}) \quad (19)$$

is the density of the single-particle levels per energy unit,  $\varepsilon_{\text{F}}$  is the Fermi energy and  $\varepsilon_{\nu}$  is the energy of a single-particle level  $\nu$ .

The "smooth" microscopic energy  $\tilde{E}_{\text{micro}}$  is defined by means of the "smooth" density of the single-particle levels  $\tilde{\rho}(\varepsilon)$ :

$$\tilde{E}_{\text{micro}} = \int_{-\infty}^{\tilde{\varepsilon}_{\text{F}}} \tilde{\rho}(\varepsilon) \varepsilon d\varepsilon. \quad (20)$$

The value of  $\tilde{\varepsilon}_{\text{F}}$ , found from the following condition for the particle number  $N$ :

$$N = \int_{-\infty}^{\varepsilon_{\text{F}}} \rho(\varepsilon) d\varepsilon = \int_{-\infty}^{\tilde{\varepsilon}_{\text{F}}} \tilde{\rho}(\varepsilon) d\varepsilon, \quad (21)$$

is in general different from the Fermi energy  $\varepsilon_{\text{F}}$ .

The "smooth" density, appearing in (20) and (21), is obtained as

$$\tilde{\rho}(\varepsilon) = \frac{1}{\gamma} \int_{-\infty}^{\infty} \rho(\varepsilon') f_p \left( \frac{\varepsilon' - \varepsilon}{\gamma} \right) d\varepsilon', \quad (22)$$

where  $f_p$  is a folding function of the Gaussian type, taken as the formal expansion of the  $\delta$ -function, truncated to the first  $2p$  terms:

$$f_p(x) = \frac{1}{\sqrt{\pi}} \sum_{n=0}^{2p} C_n H_n(x) e^{-x^2}, \quad (23)$$

with

$$C_n = \frac{1}{2^n n!} H_n(0) = \begin{cases} \frac{(-1)^{\frac{n}{2}}}{2^n (\frac{n}{2})!} & \text{for even } n \\ 0 & \text{for odd } n. \end{cases} \quad (24)$$

The width  $\gamma$  is of the order of shell energy gaps. Using  $f_p$  one obtains the averaged density  $\tilde{\rho}$ :

$$\tilde{\rho}(\varepsilon) = \frac{1}{\gamma \sqrt{\pi}} \sum_{\nu=1} e^{-u_\nu^2} \sum_{n=0}^{2p} C_n H_n(u_\nu), \quad (25)$$

where  $u_\nu = (\varepsilon - \varepsilon_\nu)/\gamma$ .

The energy (20) in general depends on the parameters  $\gamma$  and  $p$ . The method is meaningful, if there is a certain interval of  $\gamma$  and corresponding  $p$ , for which the energy does not practically depend on them (so called "plateau condition"). Here, we use  $\gamma = 1.2\hbar\omega_0$  for the Strutinski smearing parameter and a sixth-order correction polynomial for  $f_p$ .

### 2.2.3. Pairing correlations

In this work, pairing is included within the Bardeen-Cooper-Schrieffer (BCS) theory [48]. We assume a constant matrix element  $G$  of the (short-range) monopole pairing interaction. The hamiltonian of a system of nucleons, separately for neutrons and protons, may be written as:

$$H = \sum_{\nu} \varepsilon_{\nu} a_{\nu}^{\dagger} a_{\nu} - G \sum_{\nu, \nu' > 0} a_{\nu}^{\dagger} a_{\nu'}^{\dagger} a_{\bar{\nu}'} a_{\bar{\nu}}, \quad (26)$$

where  $\varepsilon_{\nu}$  denotes the energy of a single-particle state  $\nu$ . Each state  $\nu$  has its time-reversal-conjugate  $\bar{\nu}$  with the same energy (Kramers degeneration).

As the BCS wave function is a superposition of components with different numbers of particles, one requires that the expectation value of the particle number has a definite value  $N$ :

$$\langle \hat{N} \rangle = 2 \sum_{\nu > 0} v_{\nu}^2 = N. \quad (27)$$

The occupation numbers are given by

$$v_{\nu}^2 = \frac{1}{2} [1 - (\varepsilon_{\nu} - \lambda)/E_{\nu}], \quad (28)$$

where

$$E_{\nu} = \sqrt{(\varepsilon_{\nu} - \lambda)^2 + \Delta^2}. \quad (29)$$

The parameters  $\lambda$  and  $\Delta$  are solutions of the system of two equations, for the average particle number and the pairing gap:

$$N = \sum_{\nu > 0} \left[ 1 - \frac{\varepsilon_{\nu} - \lambda}{\sqrt{(\varepsilon_{\nu} - \lambda)^2 + \Delta^2}} \right] \quad (30)$$

$$\frac{2}{G} = \sum_{\nu > 0} \frac{1}{\sqrt{(\varepsilon_{\nu} - \lambda)^2 + \Delta^2}}. \quad (31)$$

For the energy of the system in the BCS state, one gets:

$$E_{\text{BCS}} = 2 \sum_{\nu > 0} \varepsilon_{\nu} v_{\nu}^2 - \frac{\Delta^2}{G} - G \sum_{\nu > 0} v_{\nu}^4. \quad (32)$$

#### 2.2.4. Pairing correction

Pairing correction energy  $E_{\text{corr}}^{\text{pair}}$  is usually constructed in analogy to the shell correction energy  $E_{\text{corr}}^{\text{sh}}$ ,

$$E_{\text{corr}}^{\text{pair}} = E_{\text{pair}} - \tilde{E}_{\text{pair}}, \quad (33)$$

where  $E_{\text{pair}}$  is the pairing energy corresponding to real single-particle level distribution  $\rho(\varepsilon)$ , Eq. (19), and  $\tilde{E}_{\text{pair}}$  is this energy for the smoothed s.p. level distribution,  $\tilde{\rho}(\varepsilon)$ , Eq. (22).

The  $E_{\text{pair}}$  is

$$E_{\text{pair}} = E_{\text{BCS}} - E_{\text{BCS}}^{\Delta=0}, \quad (34)$$

where  $E_{\text{BCS}}^{\Delta=0}$  is the  $E_{\text{BCS}}$  energy in the limit of disappearing pairing correlations ( $\Delta = 0$ ). Thus, using Eq. (32),

$$E_{\text{BCS}}^{\Delta=0} = 2 \sum_{\nu=1}^{N/2} \varepsilon_{\nu} - \frac{GN}{2}. \quad (35)$$

because for  $\Delta = 0$ , the probability  $v_{\nu}^2$  of the occupation of any state  $\nu$  is either 0 or 1.

The smoothed pairing energy term is included in a schematic form, resulting from a model with a constant level density of pairs (doubly degenerate levels)  $\bar{\rho}$ , taken equal to  $\tilde{\rho}(\varepsilon_{\text{F}})/2$

$$\tilde{E}_{\text{pair}} = -\frac{N_p^2}{\bar{\rho}}(\sqrt{1+x^2}-1) + \frac{\bar{G}N_p x}{2} \arctan(1/x). \quad (36)$$

In the above expression,  $x = \bar{\rho}\bar{\Delta}/N_p$ ,  $N_p = N/2$  is a number of pairs,  $\bar{\Delta}$  is an average value of the pairing gap in the neighbourhood of a studied nucleus, related to the average pairing strength  $\bar{G}$  via the BCS formula for a constant level density

$$\frac{1}{\bar{G}\bar{\rho}} = \ln \left( \frac{\sqrt{1+x^2}+1}{x} \right). \quad (37)$$

The values of  $\bar{\Delta}$  are taken from the fit [46]

$$\bar{\Delta} = \frac{5.72}{N^{1/3}} \exp(-0.119I - 7.89I^2) \quad (38)$$

for neutrons and

$$\bar{\Delta} = \frac{5.72}{Z^{1/3}} \exp(0.119I - 7.89I^2), \quad (39)$$

for protons, with  $I = (N - Z)/A$ . The smoothed pairing energy term calculated in this way shows nearly no deformation dependence, for example, it varies by about 50 keV over the whole deformation range in actinides. Thus, it could be omitted in energy landscapes, while it shows up in binding energies.

The pairing interaction strengths  $G$ , Eq. (26), are taken as

$$G_l = (g_{0l} + g_{1l}I)/A, \quad (40)$$

where the index  $l$  stands for p (protons) or n (neutrons).

The strengths  $G_l$  were fixed by adjusting the gap parameter  $\Delta$  to the three-point odd-even mass differences

$$\Delta_Z M = (-1)^Z \left\{ \frac{1}{2} [M(Z+1, N) + M(Z-1, N)] - M(Z, N) \right\},$$

$$\Delta_N M = (-1)^N \left\{ \frac{1}{2} [M(Z, N+1) + M(Z, N-1)] - M(Z, N) \right\}.$$

The adjustment, using all measured masses of nuclei with  $Z \geq 88$ , resulted in the values [42]:

$$\begin{aligned} g_{0l} &= 17.67 \text{ MeV}, & g_{1l} &= -13.11 \text{ MeV}, & \text{for } l = n \text{ (neutrons)}, \\ g_{0l} &= 13.40 \text{ MeV}, & g_{1l} &= 44.89 \text{ MeV}, & \text{for } l = p \text{ (protons)}. \end{aligned} \quad (41)$$

### 3. Shape parametrization

The essential point of any microscopic-macroscopic study is the kind and dimension of the deformation space used to describe a variety of nuclear shapes. This is particularly important for finding the saddle point along a fission path. Of course, there is no ideal shape parametrization. As far as we are interested in superheavy nuclei, with comparatively short fission barriers, a traditional expansion of the nuclear radius in spherical harmonics [49], can be used. We admit shapes of a 10D manifold defined by:

$$\begin{aligned} R(\vartheta, \varphi) = R_0 c(\{\beta\}) \{ & 1 + \beta [\cos \gamma Y_{20} + \sin \gamma Y_{22}^{(+)}] \\ & + \beta_{40} Y_{40} + \beta_{42} Y_{42}^{(+)} + \beta_{44} Y_{44}^{(+)} \\ & + \beta_{30} Y_{30} + \beta_{50} Y_{50} + \beta_{70} Y_{70} \\ & + \beta_{60} Y_{60} + \beta_{80} Y_{80} \} \}. \end{aligned} \quad (42)$$

The real spherical harmonics  $Y_{lm}^{(+)}$  are defined as:

$$Y_{lm}^{(+)} = \frac{1}{\sqrt{2}} [Y_{lm} + (-1)^m Y_{l-m}], \quad \text{for } m \neq 0. \quad (43)$$

We use the conventional notation:

$$\begin{aligned} \beta_{20} &= \beta \cos \gamma, \\ \beta_{22} &= \beta \sin \gamma, \end{aligned} \quad (44)$$

where  $\gamma$  is the Bohr quadrupole non-axiality parameter. The function  $c(\{\beta\})$  is determined by the volume-conservation condition.

There is no physical principle which would forbid nonaxial ground-state nuclear shapes. However, calculations by Möller et al. [50] and our studies [51–53] suggest that in the investigated nuclei the effect of nonaxiality (including octupole  $Y_{32}^+$ ) in ground states is either small or non-existent. On the other hand, competing axially symmetric minima are frequent [54]. Therefore, we assumed here the axial symmetry of the ground states. The energy is minimized simultaneously in all axial degrees of freedom:  $\beta_{20}, \beta_{30}, \beta_{40}, \beta_{50}, \beta_{60}, \beta_{70}, \beta_{80}$ , using a multidimensional conjugate gradient method.

The saddle point is defined as a *minimum* over all paths connecting the ground state with the behind-the barrier region of the *maximal* energies along each path. Practical calculations are performed as follows. Energy is calculated at the following grid points (with steps given in parentheses):

$$\begin{aligned} \beta \cos \gamma &= 0(0.05)0.65, \\ \beta \sin \gamma &= 0(0.05)0.40, \\ \beta_{40} &= -0.20(0.05)0.20. \end{aligned} \quad (45)$$

Then, energy is interpolated (by the standard SPLIN3 procedure of the IMSL library) on the grid five times denser in each direction. Thus, we finally have energy values at a total of 110946 grid points. In order to find the saddle point a two-step method is used. First, on such a 3-dimensional grid  $(\beta_{20}, \beta_{22}, \beta_{40})$ , the saddle point is determined by the Dynamic Programming Method given in [55] and adopted to the fission process by Baran et al. [56]. Then, with these three deformations fixed, energy is minimized with respect to the other degrees of freedom:  $\beta_{42}, \beta_{44}, \beta_{30}, \beta_{50}, \beta_{60}, \beta_{70}, \beta_{80}$ . In the previous calculations [57, 58], the nonaxial hexadecapole deformations have usually been treated as functions of the quadrupole triaxiality angle  $\gamma$ . In the present calculations, the hexadecapole nonaxialities  $\beta_{42}$  and  $\beta_{44}$  are independent variables.

#### 4. Dynamic programming method

It is always possible to convert an  $m$ -dimensional grid:  $(n_1 \times n_2 \times n_3 \times \dots \times n_m)$  into a four dimensional grid:  $(n_1 \times n_2 \times n_3 \times N)$ ,  $N = n_4 \times n_5 \times n_6 \times \dots \times n_m$ . In the case of our deformation space:  $n_1$  refers to  $\beta_{20}$  (elongation),  $n_2$  to  $\gamma$  (nonaxility),  $n_3$  to  $\beta_{40}$  (neck). The  $N$  - axis describes all other degrees of freedom which we use for the description of shapes (all other multipolarities). Each path  $i$ , connecting the starting point with a behind-the-barrier point  $n+1$ , may be characterized by the maximal value of energy  $E_{max}^i$  which one can find along it, where  $i$  is the index of a given path. The energy values between two neighboring points on a given path are investigated with the help of an interpolation procedure. In this way, we have a set of all possible paths  $i$ , connecting the starting point to the  $n+1$ -th point, with the value of the maximal energy  $E_{max}^i$  on each. It is obvious that the saddle-point energy will be the minimal value of all  $E_{max}^i$  over all possible paths (all possible  $i$ ). The trajectory corresponding to this minimal value will automatically pass through the saddle point. It appears that to find the right trajectory along which  $E_{max}^i$  is minimal we do not need to consider all possible trajectories.

#### 5. Numerical tests and error checks

The important numerical tool exploited here is the minimization procedure. It is used to find the ground state energy in a 7-dimensional space and the saddle point energy by the 7-dimensional minimization. Multidimensional minimization is a mixed blessing method: from the one point of view, it gives us the opportunity to find minima in the large deformation spaces (infeasible on a grid) but from the other, it introduces the necessity to check whether or not, the obtained minima are indeed the global ones. In order to gain some confidence in our results we used a number of checks. The standard checks within the minimization routine include the monitoring of energy gradients. In addition, we looked at the continuity of the resulting deformation parameters with respect to  $\beta \sin \gamma$  and  $\beta \cos \gamma$  and at their stability with respect to the choice of their starting values. The starting values of the deformation parameters were always taken different from zero.

It should be also realized that we cannot be absolutely certain that the minimization in the second step of our saddle-point-search procedure does not lead to errors. The hope that the initial deformation net  $(\beta \sin \gamma, \beta \cos \gamma, \beta_{40})$  may be sufficient is based mainly on the fact that other deformations are small and weakly coupled to those three. In addition, we have checked saddle point energies obtained in the first stage of our procedure on the 3D grid by comparing them to the results of the analogous procedure using the 2D  $(\beta \sin \gamma, \beta \cos \gamma)$  and two variants of the 4D grids:  $(\beta \sin \gamma, \beta \cos \gamma, \beta_{40}, \beta_{42})$

Table A

5D-IFW results

| Z   | N   | E [MeV] | $\beta_{20}^{sp}$ | $\beta_{22}^{sp}$ | $\beta_{40}^{sp}$ | $\beta_{60}^{sp}$ | $\beta_{80}^{sp}$ |
|-----|-----|---------|-------------------|-------------------|-------------------|-------------------|-------------------|
| 108 | 166 | -1.05   | 0.33              | 0.01              | 0.04              | -0.01             | 0.05              |
| 112 | 174 | -0.48   | 0.27              | 0.01              | -0.04             | 0.04              | 0.02              |

and  $(\beta \sin \gamma, \beta \cos \gamma, \beta_{40}, \beta_{44})$ . An important test of the saddle-point searching method was the application of a completely different approach based on so-called "*imaginary water flow*" (IWF) [59–63]. This conceptually simple method is still numerically efficient in the 5-dimensional space of deformations  $\beta \sin \gamma, \beta \cos \gamma, \beta_{40}, \beta_{60}, \beta_{80}$  and has been used for some nuclei. In order to avoid ambiguity, saddle points with vanishing parameters:  $\beta_{42}, \beta_{44}$  were chosen. The obtained results were practically identical with those of the previous method as one can see in Table A. One can see that the difference in barrier does not exceed 110 keV.

## 6. Discussion of the results

The calculated properties of ground-states of even-even nuclei are given in Table 1 and those of saddle-points in Table 2. Energy maps in  $(\beta \cos \gamma, \beta \sin \gamma)$  plane, necessary to appreciate fission barriers, are shown in Fig. 1. They were obtained by minimization over 8 remaining deformations. Total energy shown in Tables and Figures is normalized in such a way that its macroscopic part is equal zero at the spherical shape.

### 6.1. Ground state properties

To find the ground state masses and shapes the total energy is minimized (using the gradient method) with respect to  $\beta_{20}, \beta_{30}, \beta_{40}, \beta_{50}, \beta_{60}, \beta_{70}, \beta_{80}$ . The candidates for the global minimum are chosen from the energy map  $(\beta_{20}, \beta_{22})$  by inspection, taking into account barriers heights. Only in a few cases we obtained a small nonzero value of the octupole deformation and these are not given in Tables. Macroscopic and microscopic parts of total energy are shown in Fig. 3. The biggest shell effect ( $\sim 9$  MeV) is observed for  $^{270}\text{Hs}$  ( $Z = 108, N = 162$ ), the semi-magic nucleus. As in other Woods-Saxon micro-macro calculations, the second minimum ( $\sim 7$  MeV) of the shell correction is located around the nucleus  $Z = 114$  and  $N = 184$ . When superposed with weakly deformation-dependent macroscopic part (Fig.3), this component is largely responsible for the emergence of global minima in superheavy nuclei.

#### 6.1.1. Ground state shapes (deformations)

As mentioned in section 3, calculations including nonaxial shapes show that the ground states are usually axially symmetric. For  $Z > 120$ , there are a few minima exhibiting unusual shapes [54], but they are at most degenerate with the minima given in Table 1. In addition to typical prolate, spherical and oblate shapes, the superdeformed oblate (SDO) shapes with  $\beta_{20} \approx -0.45$  appear for some  $Z \approx 120$  nuclei, discussed in the recent work [65].

In the studied nuclei, up to  $Z = 118$ , the shape evolution starts with prolate shapes for small  $N$  and ends with oblate or spherical (close to  $N = 184$ ) for largest  $N$ . The neutron-deficient  $Z \geq 120$  nuclei have SDO ground states. With increasing  $N$ , they evolve into oblate, then spherical, then oblate again, but for  $Z = 126$  all ground states are oblate. In some  $Z \geq 120$  systems, SDO ground states reappear for largest  $N$  - see Fig. 1.

Table B

Statistical parameters of the calculated mass excess in relation to experimental or recommended atomic mass excess [64]. All quantities are in MeV, except for the number of nuclei  $N$ .

| $N$ | $\langle  M_{gs}^{th} - M_{gs}^{exp}  \rangle$ | $Max  M_{gs}^{th} - M_{gs}^{exp} $ | r.m.s |
|-----|--|------------------------------------|-------|
| 67  | 0.43   | 1.58                               | 0.58  |

Energy maps are necessary to study secondary minima and appreciate the competition of various shapes. The competition of prolate, spherical and oblate minima in  $Z = 120$  nuclei may be seen in Fig. 1. Let us note that the apparent secondary prolate minima at  $\beta_{20} \approx 0.4$  are so shallow that they cannot be seriously considered as candidates for equilibrium configurations. In neutron deficient isotopes, the prolate and SDO shapes compete. With increasing  $N$ , the prolate minimum disappears and normal oblate minimum becomes lower than the SDO minimum. The spherical configuration becomes the g.s. for  $N = 180 - 184$ . For still heavier isotopes (Table 1, not shown in Fig.1), the SDO minimum reappears as the g.s.

In Fig. 2, energy landscapes are shown for three experimental nuclei (one synthesized in GSI and two in Dubna) and one hypothetical  $Z = 124$  system. The  $^{276}\text{Ds}$  is prolate, the two heavier,  $^{286}114$  and  $^{294}118$ , are weakly deformed and  $\gamma$ -soft, while  $^{308}124$  is weakly oblate.

#### 6.1.2. Ground state mass excess

The accuracy of the approach may be assessed by comparing calculated and experimental masses (ground state masses)[64]. The difference  $M_{gs}^{th} - M_{gs}^{exp}$  is shown in Fig. 4 as a function of  $A$  and in Fig. 5 as a function of both  $Z$  and  $N$ . The accuracy is summarized in Table B below. The average discrepancy  $\langle |M_{gs}^{th} - M_{gs}^{exp}| \rangle$ , the maximal difference  $Max |M_{gs}^{th} - M_{gs}^{exp}|$  and the *r.m.s.* deviation are shown for a number  $N$  of even-even superheavy nuclei.

The agreement between the calculated and experimental masses is the worst for nuclei located near  $Z = 106$ ,  $N = 162$  ( $\simeq +1.5$  MeV) and  $Z = 114$ ,  $N = 184$  ( $\simeq -1.5$  MeV).

#### 6.1.3. $Q$ -alpha energies

$Q_{\alpha}^{th}$  values given in Table 2 are calculated always for g.s. to g.s transitions, even if the corresponding deformations differ widely and hence one can expect a substantial decay hindrance.  $Q_{\alpha}$  energy for a nucleus with  $N$  neutrons and  $Z$  protons can be directly obtained from masses

$$Q_{\alpha}^{th}(Z, N) = M_{gs}^{th}(Z, N) - M_{gs}^{th}(Z-2, N-2) - M(2, 2). \quad (46)$$

The resulting discrepancies between calculated and experimental  $Q_{\alpha}$  values are shown in Table C. The average discrepancy  $\langle |Q_{\alpha}^{th} - Q_{\alpha}^{exp}| \rangle$ , the maximal difference  $Max |Q_{\alpha}^{th} - Q_{\alpha}^{exp}|$  and the *r.m.s.* deviation are shown for a number  $N$  of even-even superheavy nuclei.

The largest discrepancy between the calculated and experimental  $Q_{\alpha}$  values results for nuclei located near  $Z = 106$ ,  $N = 162$ , what is a consequence of the calculated masses in this area.



Table C

Statistical parameters of calculated  $Q_\alpha$  energies in relation to experimental data [64]. All quantities are in MeV, except for the number of nuclei N.

| N  | $\langle  Q_\alpha^{th} - Q_\alpha^{exp}  \rangle$ | $Max  Q_\alpha^{th} - Q_\alpha^{exp} $ | r.m.s |
|----|--|--|-------|
| 67 | 0.02   | 0.74                                   | 0.29  |

### 6.2. Saddle point properties

It is worth emphasizing that the saddles listed in Table 2 correspond to the ground states. In case that secondary minima exist, their saddle points may be *different* from that of the ground state. In other words, a saddle point always relates to a minimum (equilibrium, metastable state) whose decay it characterizes.

The used method of the search for saddles, the combined 3D saddle-point search and subsequent 7D minimization, implies that they may slightly differ from those read from the maps in  $(\beta \cos \gamma, \beta \sin \gamma)$ , shown in Figs. 2 and 3. The latter are fixed by the single 8D minimization for the purpose of illustration of an energy landscape. For example, the axially-symmetric saddle in  $^{288}120$  seems to be lower than the triaxial one in Fig. 2, while it is the opposite in Table 2. The local shell correction and the macroscopic energy at the saddle point configuration has been shown in Fig. 9. Generally, we see that the shell effects at the saddle point are much weaker than in the ground state, but not negligible. The most pronounced effects ( $\sim 3$  MeV) were obtained around nuclei with  $Z=102$ ,  $N=162$  and  $Z=114$ ,  $N=184$ . For the majority of nuclei, microscopic energy at the saddle point is negative while macroscopic energy is positive. Values of these energies are similar in magnitude.

#### 6.2.1. Saddle point shapes (deformations)

The calculated saddles are mostly triaxial in  $Z = 98 - 104$ , and exclusively triaxial in  $Z \geq 122$  nuclei. There are many triaxial saddles with rather sizable values of the deformation  $\gamma$ . Since the saddle deformation is a result of a competition between the axial and triaxial saddle energies, even their tiny difference may result in an abrupt change in  $\gamma^{sp}$ . This is reflected in the abrupt changes of  $\gamma^{sp}$  between neighbouring isotopes - Table 2. Stated otherwise, a large  $\gamma^{sp}$  does not necessarily correlate with a large nonaxiality effect on the saddle-point energy (mass).

#### 6.2.2. Saddle point mass excess - fission barriers

Fission barriers may be obtained from Tables 1 and 2 as:

$$B_f = E_{sp}^{th} - E_{gs}^{th} = M_{sp}^{th} - M_{gs}^{th}. \quad (47)$$

Most of them were given and discussed in [66]. One can compare our barriers heights with other recent calculations [63, 67–70]. They are relevant for fission rates from excited states (thermal rates), with the excitation energy greater than, roughly, the barrier itself. The spontaneous fission rates involve an additional inertia effect, see e.g. [71].

## 7. Summary

Using the macroscopic-microscopic model, we have calculated the ground state and saddle point properties of even-even superheavy elements: masses, macroscopic energies, shell corrections, deformations as well as the ground state to

ground state alpha decay energies.

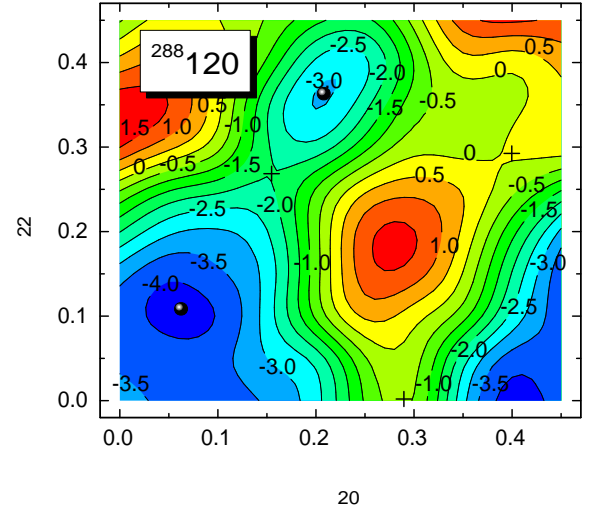
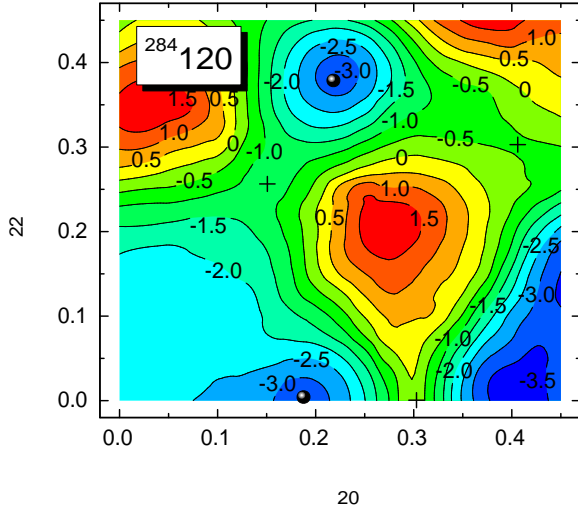
## Acknowledgments

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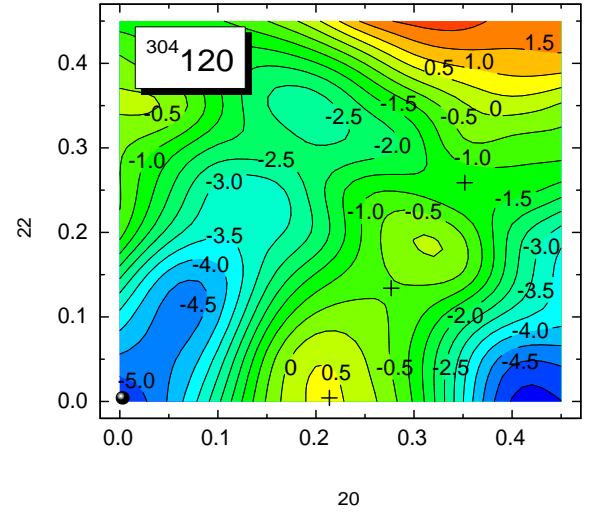
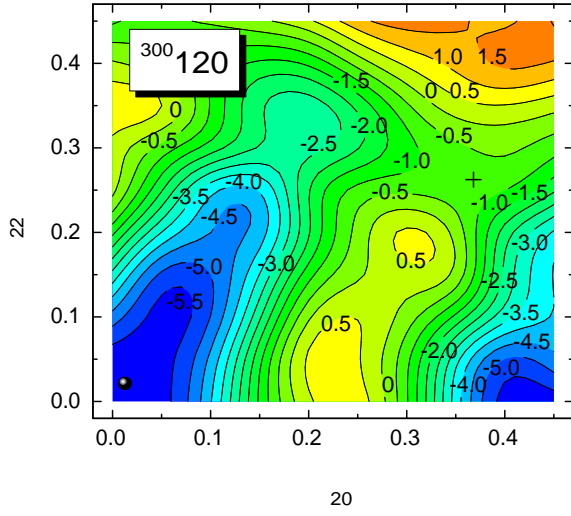
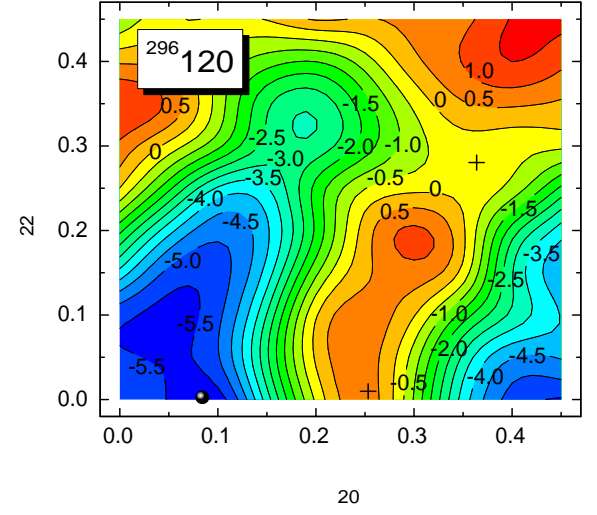
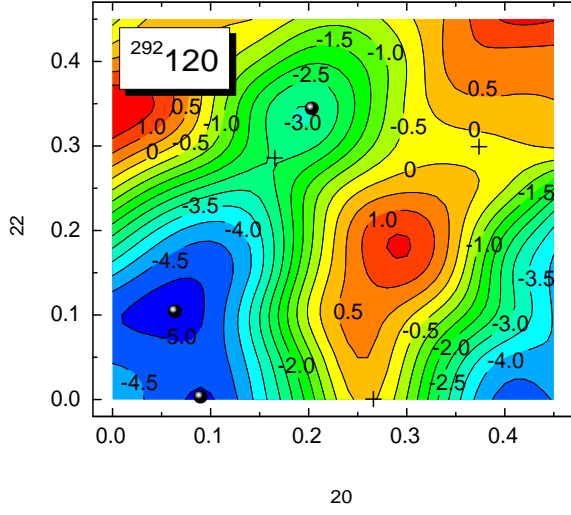
**Table 1. Ground state properties**

For the isotopes of the elements  $Z=98-126$ , tabulates the ground state masses, total energies, macroscopic and microscopic energies, equilibrium deformations and corresponding  $\alpha$ -decay ground state to ground state  $Q$ -values.

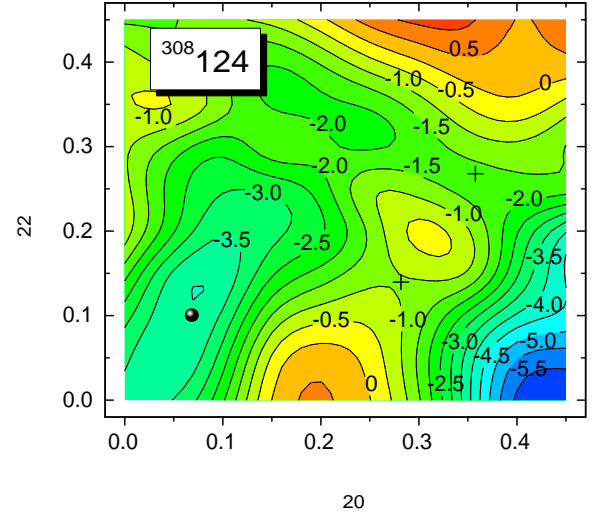
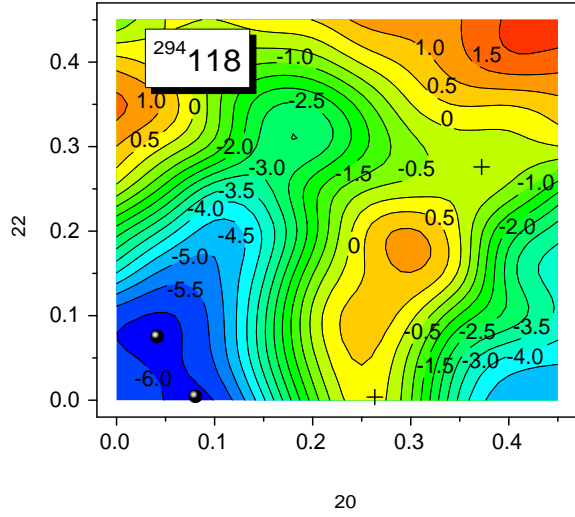
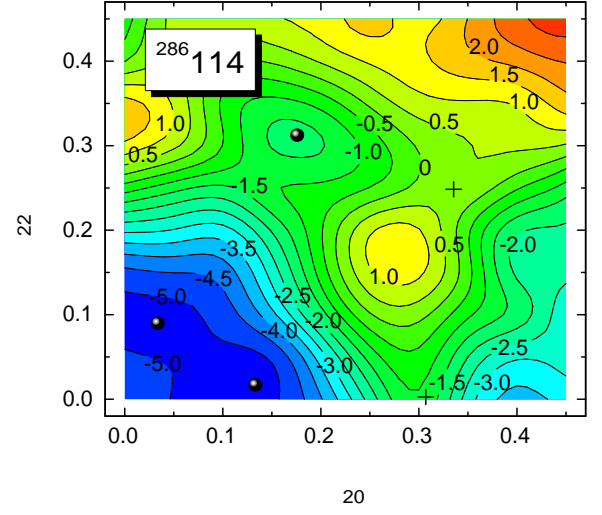
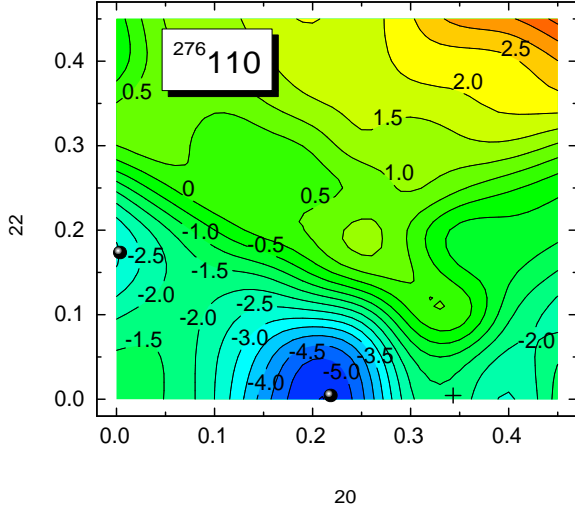
|  |                               |
|--|-------------------------------|
| $Z$                                      | The atomic number             |
| $A$                                      | The mass number               |
| $M_{gs}^{th}$                            | The mass excess in MeV        |
| $E$                                      | The total energy in MeV       |
| $E_{mac}$                                | The macroscopic energy in MeV |
| $E_{mic}$                                | The microscopic energy in MeV |
| $\beta_{20}^{min} \div \beta_{80}^{min}$ | The equilibrium deformations  |
| $Q_{\alpha}$                             | Theoretical $Q$ -value in MeV |



■



**Fig. 1:** Energy surfaces,  $E - E_{mac}(sphere)$ , for  $Z = 120$  isotopes, resulting from the minimization over the remaining 8 deformations.



**Fig. 2:** As in Fig. 1, but for the three of experimentally detected evaporation residues and one hypothetical heavier system.

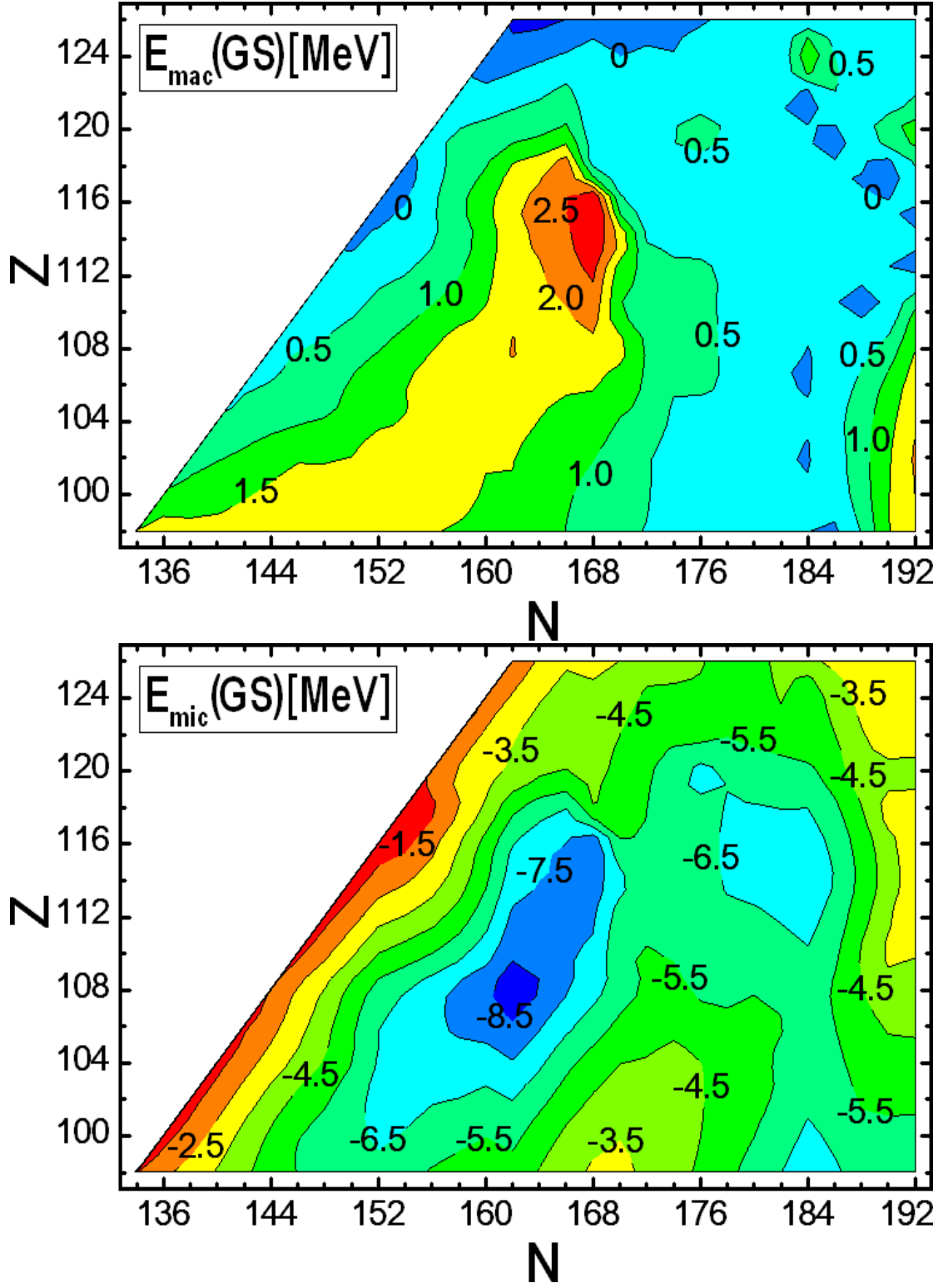


Fig. 3: Calculated macroscopic and microscopic components of the ground-state binding energy,  $E_{\text{mac}} - E_{\text{mac}}(\text{sphere})$  and  $E_{\text{micr.}}$ .

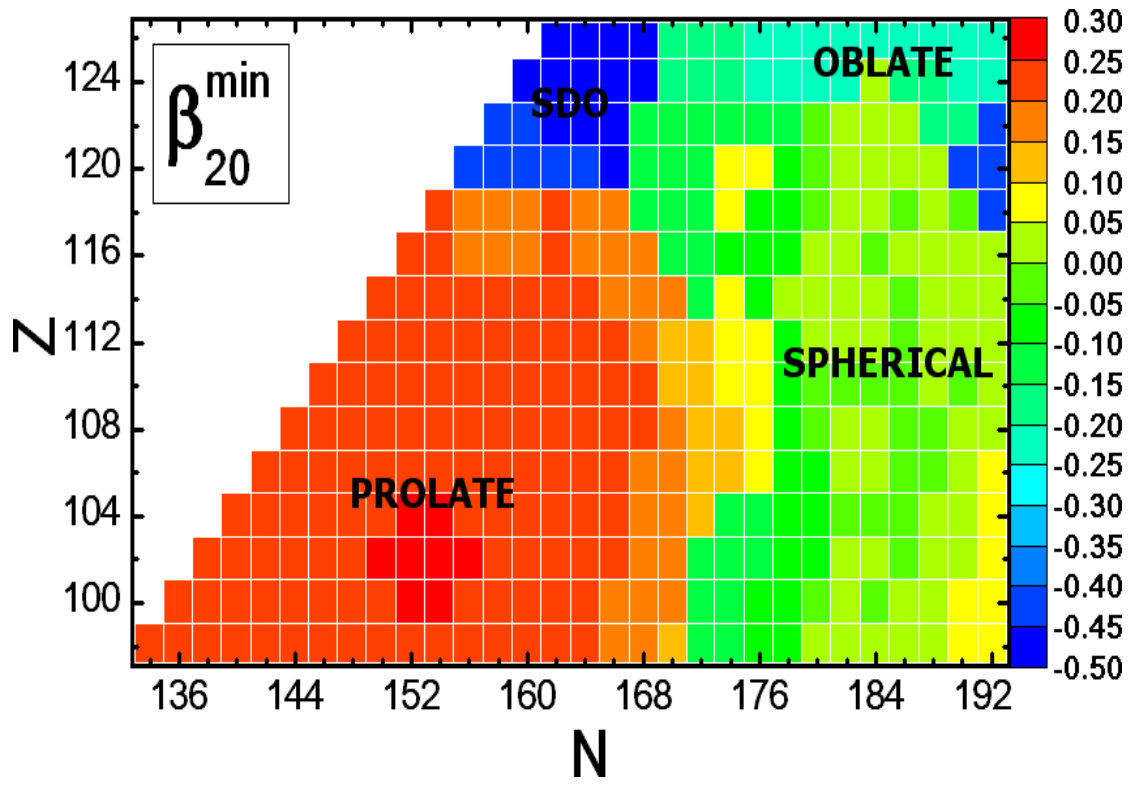
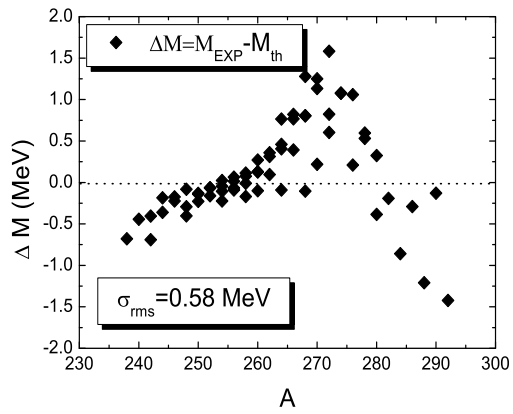
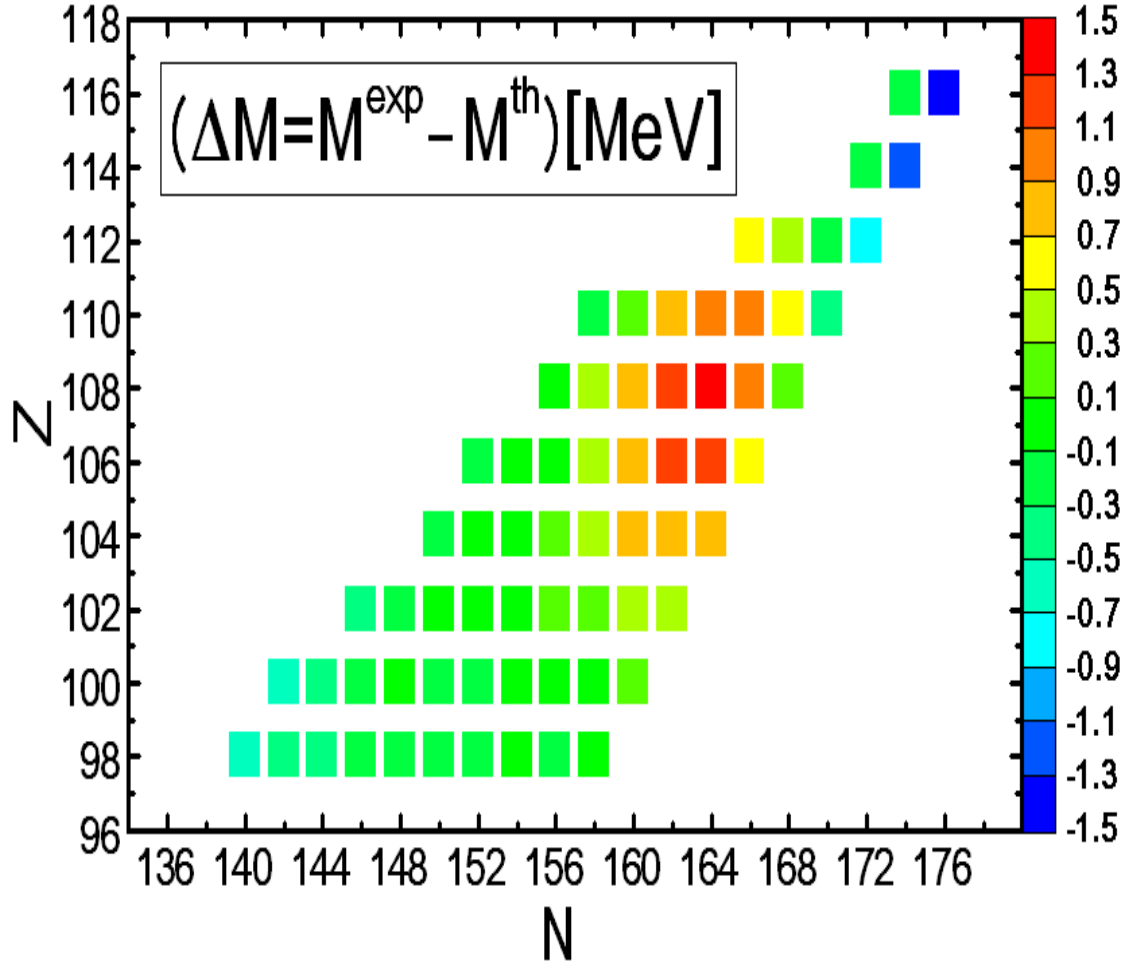


Fig. 4: Calculated ground-state quadrupole deformations.



**Fig. 5:** Discrepancy between the measured and calculated nuclear masses vs mass number.



**Fig. 6:** As in Fig. 4, but as a function of proton and neutron numbers.



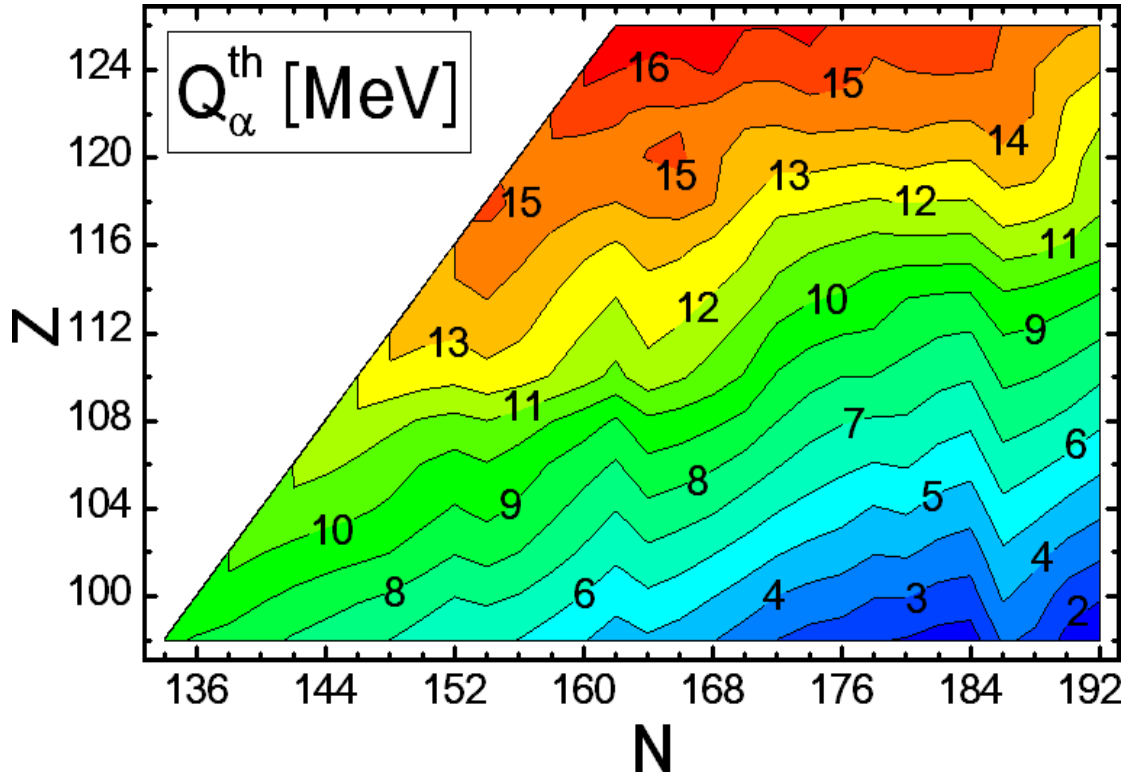


Fig. 7: Calculated  $\alpha$ -decay energies for g.s. $\rightarrow$ g.s transitions as a function of proton and neutron numbers.

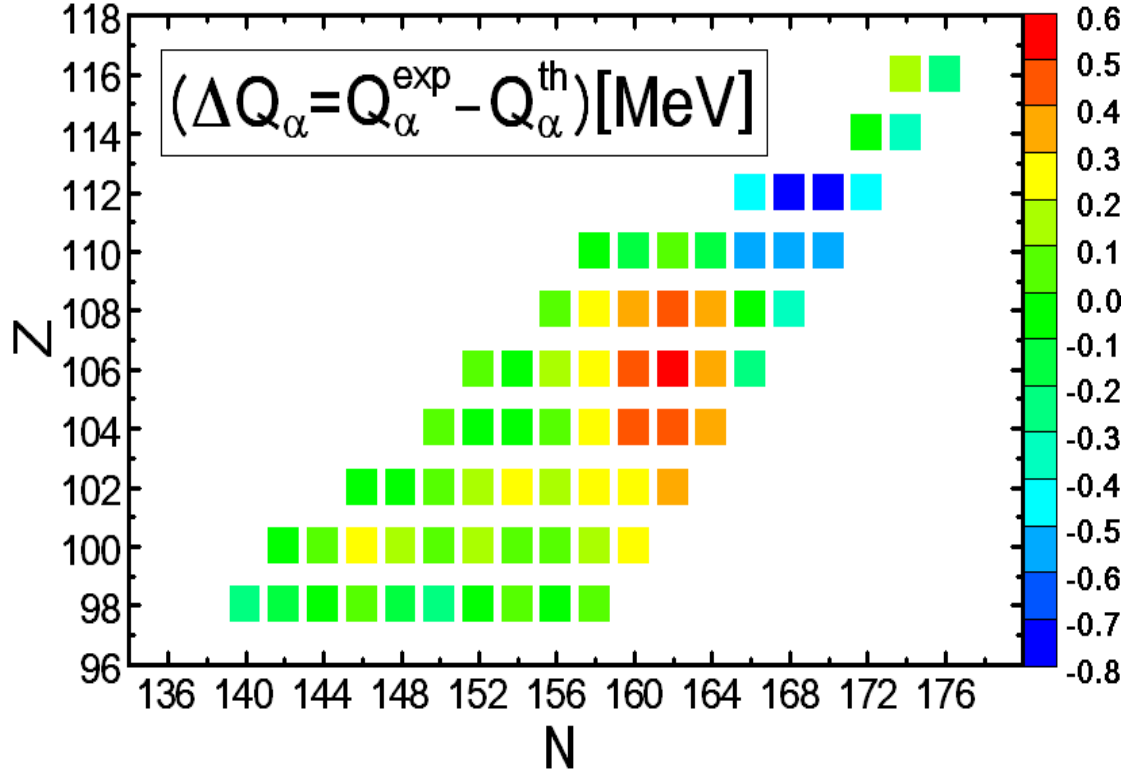


Fig. 8: Discrepancy between the experimental and calculated  $\alpha$ -decay energies as a function of proton and neutron numbers.

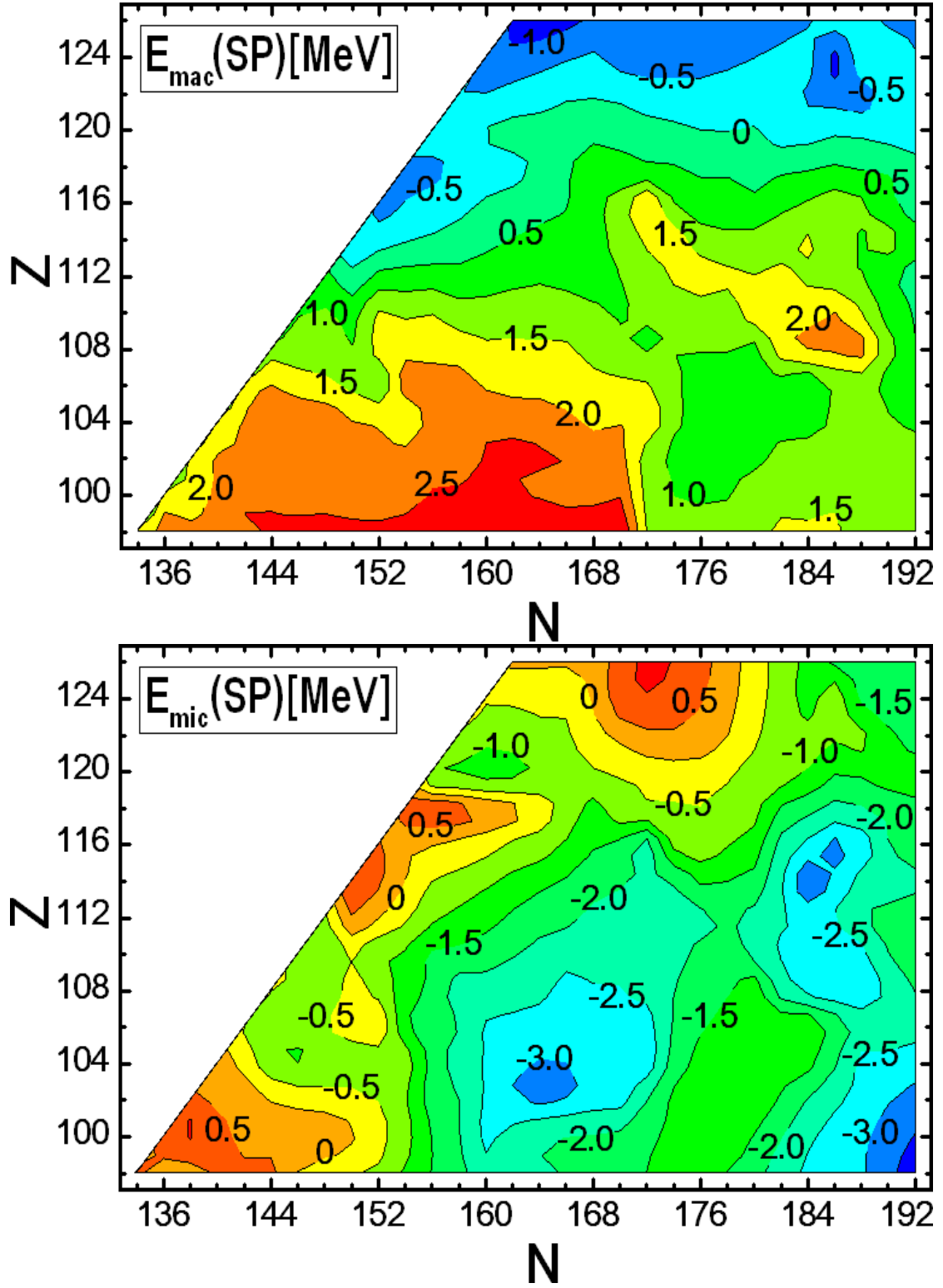


Fig. 9: As in Fig. 3, but for the calculated saddle points.

**Table 1**  
Calculated Ground State Masses and Deformations.

| Z   | N   | $M_{gs}^{th}$ | E     | $E_{mac}$ | $E_{mic}$ | $\beta_{20}^{min}$ | $\beta_{40}^{min}$ | $\beta_{60}^{min}$ | $\beta_{80}^{min}$ | $Q_{alpha}$ |
|-----|-----|---------------|-------|-----------|-----------|--------------------|--------------------|--------------------|--------------------|-------------|
| 98  | 134 | 59.53         | 0.09  | 1.54      | -1.46     | 0.210              | 0.081              | 0.009              | -0.003             | 9.289       |
| 98  | 136 | 58.38         | -0.61 | 1.68      | -2.29     | 0.209              | 0.085              | 0.007              | -0.004             | 8.883       |
| 98  | 138 | 57.86         | -1.27 | 1.67      | -2.95     | 0.214              | 0.084              | 0.001              | -0.006             | 8.653       |
| 98  | 140 | 57.88         | -1.99 | 1.66      | -3.64     | 0.221              | 0.081              | -0.007             | -0.009             | 8.286       |
| 98  | 142 | 58.48         | -2.69 | 1.68      | -4.37     | 0.226              | 0.078              | -0.014             | -0.011             | 7.883       |
| 98  | 144 | 59.74         | -3.28 | 1.73      | -5.01     | 0.234              | 0.073              | -0.023             | -0.015             | 7.567       |
| 98  | 146 | 61.66         | -3.77 | 1.82      | -5.58     | 0.240              | 0.067              | -0.030             | -0.017             | 7.232       |
| 98  | 148 | 64.32         | -4.05 | 1.67      | -5.72     | 0.242              | 0.056              | -0.035             | -0.012             | 6.987       |
| 98  | 150 | 67.53         | -4.30 | 1.50      | -5.80     | 0.242              | 0.043              | -0.038             | -0.005             | 6.574       |
| 98  | 152 | 71.30         | -4.50 | 1.60      | -6.10     | 0.247              | 0.029              | -0.046             | 0.002              | 6.138       |
| 98  | 154 | 76.10         | -4.18 | 1.56      | -5.74     | 0.248              | 0.019              | -0.046             | 0.008              | 6.215       |
| 98  | 156 | 81.45         | -3.80 | 1.52      | -5.32     | 0.244              | 0.008              | -0.045             | 0.013              | 5.966       |
| 98  | 158 | 87.13         | -3.57 | 1.42      | -4.99     | 0.238              | -0.004             | -0.041             | 0.016              | 5.503       |
| 98  | 160 | 93.12         | -3.49 | 1.35      | -4.84     | 0.235              | -0.021             | -0.032             | 0.018              | 5.055       |
| 98  | 162 | 99.36         | -3.64 | 1.46      | -5.10     | 0.223              | -0.042             | -0.022             | 0.020              | 4.526       |
| 98  | 164 | 106.70        | -3.12 | 1.12      | -4.24     | 0.209              | -0.039             | -0.013             | 0.013              | 4.843       |
| 98  | 166 | 114.39        | -2.70 | 0.94      | -3.65     | 0.191              | -0.040             | -0.005             | 0.008              | 4.528       |
| 98  | 168 | 122.20        | -2.60 | 0.71      | -3.30     | 0.165              | -0.035             | -0.001             | 0.005              | 4.042       |
| 98  | 170 | 130.12        | -2.81 | 0.51      | -3.32     | 0.141              | -0.029             | 0.001              | 0.003              | 3.532       |
| 98  | 172 | 138.08        | -3.40 | 0.46      | -3.86     | -0.138             | 0.018              | 0.009              | -0.006             | 2.988       |
| 98  | 174 | 146.37        | -4.07 | 0.28      | -4.35     | -0.115             | 0.008              | 0.006              | -0.003             | 2.621       |
| 98  | 176 | 155.15        | -4.64 | 0.20      | -4.84     | -0.097             | -0.003             | 0.007              | 0.001              | 2.480       |
| 98  | 178 | 164.18        | -5.36 | 0.22      | -5.58     | -0.088             | -0.010             | 0.010              | 0.004              | 2.069       |
| 98  | 180 | 173.71        | -5.96 | 0.01      | -5.97     | 0.003              | 0.000              | 0.000              | 0.000              | 1.928       |
| 98  | 182 | 183.40        | -6.79 | 0.01      | -6.80     | 0.000              | 0.001              | 0.000              | 0.000              | 1.647       |
| 98  | 184 | 193.60        | -7.47 | 0.01      | -7.48     | 0.000              | 0.000              | 0.000              | 0.000              | 1.509       |
| 98  | 186 | 206.10        | -6.22 | 0.04      | -6.25     | 0.000              | 0.000              | 0.000              | 0.000              | 3.152       |
| 98  | 188 | 218.92        | -5.00 | 0.94      | -5.93     | 0.028              | 0.013              | 0.002              | -0.001             | 2.786       |
| 98  | 190 | 231.48        | -4.40 | 1.81      | -6.21     | 0.056              | 0.031              | 0.004              | -0.003             | 1.669       |
| 98  | 192 | 244.29        | -3.88 | 2.05      | -5.94     | 0.066              | 0.032              | 0.001              | -0.003             | 1.005       |
| 100 | 136 | 71.84         | -0.06 | 1.11      | -1.17     | 0.231              | 0.065              | -0.009             | -0.006             | 9.885       |
| 100 | 138 | 70.38         | -0.80 | 1.21      | -2.02     | 0.232              | 0.066              | -0.015             | -0.007             | 9.567       |
| 100 | 140 | 69.44         | -1.60 | 1.32      | -2.92     | 0.233              | 0.066              | -0.020             | -0.009             | 9.156       |
| 100 | 142 | 69.09         | -2.40 | 1.47      | -3.87     | 0.236              | 0.066              | -0.026             | -0.011             | 8.784       |
| 100 | 144 | 69.37         | -3.13 | 1.60      | -4.73     | 0.240              | 0.062              | -0.033             | -0.014             | 8.467       |
| 100 | 146 | 70.31         | -3.76 | 1.75      | -5.51     | 0.245              | 0.057              | -0.040             | -0.015             | 8.146       |
| 100 | 148 | 71.99         | -4.19 | 1.66      | -5.85     | 0.247              | 0.047              | -0.044             | -0.009             | 7.900       |
| 100 | 150 | 74.22         | -4.61 | 1.60      | -6.20     | 0.248              | 0.034              | -0.048             | -0.002             | 7.474       |
| 100 | 152 | 76.98         | -5.00 | 1.72      | -6.72     | 0.251              | 0.023              | -0.053             | 0.004              | 7.020       |
| 100 | 154 | 80.95         | -4.70 | 1.66      | -6.36     | 0.250              | 0.013              | -0.052             | 0.009              | 7.222       |
| 100 | 156 | 85.47         | -4.35 | 1.67      | -6.01     | 0.248              | 0.001              | -0.051             | 0.016              | 6.945       |
| 100 | 158 | 90.35         | -4.12 | 1.64      | -5.76     | 0.245              | -0.012             | -0.046             | 0.020              | 6.477       |
| 100 | 160 | 95.52         | -4.09 | 1.42      | -5.51     | 0.236              | -0.026             | -0.035             | 0.019              | 5.961       |
| 100 | 162 | 100.93        | -4.27 | 1.45      | -5.72     | 0.226              | -0.044             | -0.023             | 0.019              | 5.386       |
| 100 | 164 | 107.59        | -3.67 | 1.14      | -4.80     | 0.215              | -0.041             | -0.013             | 0.013              | 5.812       |
| 100 | 166 | 114.64        | -3.13 | 1.01      | -4.14     | 0.197              | -0.044             | -0.006             | 0.008              | 5.518       |
| 100 | 168 | 121.84        | -2.88 | 0.81      | -3.68     | 0.175              | -0.040             | -0.002             | 0.005              | 5.025       |
| 100 | 170 | 129.19        | -2.92 | 0.63      | -3.54     | 0.150              | -0.037             | 0.001              | 0.002              | 4.557       |
| 100 | 172 | 136.52        | -3.38 | 0.47      | -3.85     | -0.143             | 0.017              | 0.010              | -0.007             | 3.982       |
| 100 | 174 | 144.17        | -3.95 | 0.29      | -4.24     | -0.120             | 0.007              | 0.008              | -0.003             | 3.672       |
| 100 | 176 | 152.27        | -4.48 | 0.20      | -4.68     | -0.100             | -0.004             | 0.007              | 0.001              | 3.480       |
| 100 | 178 | 160.63        | -5.15 | 0.27      | -5.42     | -0.095             | -0.014             | 0.011              | 0.006              | 3.054       |
| 100 | 180 | 169.65        | -5.55 | 0.08      | -5.62     | -0.047             | -0.011             | -0.001             | 0.000              | 3.041       |
| 100 | 182 | 178.81        | -6.19 | 0.01      | -6.20     | 0.000              | 0.001              | 0.000              | 0.000              | 2.670       |
| 100 | 184 | 188.40        | -6.78 | 0.08      | -6.85     | -0.001             | 0.002              | 0.000              | 0.000              | 2.573       |
| 100 | 186 | 200.15        | -5.58 | 0.37      | -5.94     | 0.004              | 0.002              | 0.002              | 0.000              | 4.119       |
| 100 | 188 | 212.05        | -4.59 | 1.05      | -5.64     | 0.026              | 0.014              | 0.001              | -0.001             | 3.524       |
| 100 | 190 | 223.92        | -3.98 | 1.78      | -5.76     | 0.052              | 0.028              | 0.002              | -0.003             | 2.575       |
| 100 | 192 | 236.03        | -3.49 | 2.13      | -5.62     | 0.067              | 0.030              | -0.003             | -0.003             | 2.132       |
| 102 | 138 | 84.61         | -0.33 | 0.84      | -1.17     | 0.241              | 0.049              | -0.019             | -0.008             | 10.347      |
| 102 | 140 | 82.84         | -1.11 | 0.97      | -2.08     | 0.237              | 0.052              | -0.022             | -0.009             | 10.037      |
| 102 | 142 | 81.63         | -1.92 | 1.11      | -3.03     | 0.237              | 0.053              | -0.027             | -0.011             | 9.756       |
| 102 | 144 | 81.03         | -2.69 | 1.29      | -3.98     | 0.242              | 0.051              | -0.034             | -0.012             | 9.511       |
| 102 | 146 | 81.07         | -3.38 | 1.46      | -4.83     | 0.246              | 0.046              | -0.042             | -0.012             | 9.273       |

*Continued. . .*

Table 1 contd. . .

| Z   | N   | $M_{gs}^{th}$ | E     | $E_{mac}$ | $E_{mic}$ | $\beta_{20}^{min}$ | $\beta_{40}^{min}$ | $\beta_{60}^{min}$ | $\beta_{80}^{min}$ | $Q_{alpha}$ |
|-----|-----|---------------|-------|-----------|-----------|--------------------|--------------------|--------------------|--------------------|-------------|
| 102 | 148 | 81.75         | -3.98 | 1.46      | -5.44     | 0.248              | 0.035              | -0.047             | -0.005             | 9.006       |
| 102 | 150 | 82.95         | -4.60 | 1.53      | -6.13     | 0.251              | 0.024              | -0.051             | 0.003              | 8.532       |
| 102 | 152 | 84.70         | -5.20 | 1.75      | -6.95     | 0.254              | 0.014              | -0.057             | 0.007              | 8.060       |
| 102 | 154 | 87.76         | -5.00 | 1.74      | -6.74     | 0.252              | 0.004              | -0.056             | 0.014              | 8.359       |
| 102 | 156 | 91.37         | -4.76 | 1.77      | -6.53     | 0.252              | -0.007             | -0.053             | 0.021              | 7.989       |
| 102 | 158 | 95.34         | -4.65 | 1.80      | -6.45     | 0.248              | -0.021             | -0.048             | 0.025              | 7.445       |
| 102 | 160 | 99.64         | -4.70 | 1.50      | -6.20     | 0.237              | -0.034             | -0.035             | 0.021              | 6.862       |
| 102 | 162 | 104.19        | -4.98 | 1.50      | -6.48     | 0.228              | -0.048             | -0.024             | 0.020              | 6.249       |
| 102 | 164 | 110.15        | -4.30 | 1.27      | -5.58     | 0.217              | -0.049             | -0.015             | 0.014              | 6.792       |
| 102 | 166 | 116.50        | -3.70 | 1.13      | -4.83     | 0.202              | -0.050             | -0.008             | 0.009              | 6.480       |
| 102 | 168 | 123.13        | -3.26 | 0.96      | -4.23     | 0.184              | -0.048             | -0.002             | 0.006              | 6.065       |
| 102 | 170 | 129.87        | -3.16 | 0.72      | -3.88     | 0.157              | -0.042             | 0.000              | 0.003              | 5.604       |
| 102 | 172 | 136.69        | -3.40 | 0.47      | -3.87     | -0.146             | 0.017              | 0.011              | -0.007             | 5.075       |
| 102 | 174 | 143.68        | -3.90 | 0.28      | -4.18     | -0.124             | 0.006              | 0.008              | -0.003             | 4.727       |
| 102 | 176 | 151.11        | -4.36 | 0.22      | -4.57     | -0.105             | -0.007             | 0.007              | 0.002              | 4.516       |
| 102 | 178 | 158.74        | -5.03 | 0.31      | -5.34     | -0.098             | -0.017             | 0.012              | 0.007              | 4.045       |
| 102 | 180 | 167.19        | -5.29 | 0.09      | -5.38     | -0.053             | -0.013             | -0.001             | 0.000              | 4.138       |
| 102 | 182 | 175.78        | -5.79 | 0.02      | -5.81     | 0.000              | 0.001              | 0.000              | 0.000              | 3.706       |
| 102 | 184 | 184.73        | -6.32 | 0.04      | -6.35     | 0.000              | 0.001              | 0.000              | 0.000              | 3.492       |
| 102 | 186 | 195.69        | -5.21 | 0.50      | -5.71     | -0.002             | 0.001              | 0.000              | -0.002             | 4.867       |
| 102 | 188 | 206.90        | -4.22 | 1.06      | -5.28     | 0.018              | 0.010              | 0.001              | -0.001             | 4.329       |
| 102 | 190 | 218.14        | -3.56 | 1.76      | -5.32     | 0.047              | 0.026              | 0.000              | -0.004             | 3.667       |
| 102 | 192 | 229.57        | -3.07 | 2.33      | -5.40     | 0.072              | 0.035              | -0.004             | -0.002             | 3.217       |
| 104 | 140 | 97.94         | -0.61 | 0.60      | -1.21     | 0.238              | 0.036              | -0.020             | -0.009             | 10.905      |
| 104 | 142 | 95.90         | -1.40 | 0.73      | -2.13     | 0.236              | 0.038              | -0.024             | -0.010             | 10.633      |
| 104 | 144 | 94.46         | -2.17 | 0.86      | -3.03     | 0.239              | 0.036              | -0.031             | -0.011             | 10.408      |
| 104 | 146 | 93.63         | -2.90 | 0.97      | -3.88     | 0.243              | 0.030              | -0.037             | -0.009             | 10.173      |
| 104 | 148 | 93.34         | -3.65 | 1.04      | -4.69     | 0.245              | 0.020              | -0.042             | -0.003             | 9.848       |
| 104 | 150 | 93.54         | -4.45 | 1.19      | -5.64     | 0.248              | 0.009              | -0.047             | 0.004              | 9.374       |
| 104 | 152 | 94.30         | -5.22 | 1.46      | -6.68     | 0.251              | 0.002              | -0.053             | 0.009              | 8.932       |
| 104 | 154 | 96.41         | -5.18 | 1.54      | -6.71     | 0.250              | -0.009             | -0.051             | 0.016              | 9.283       |
| 104 | 156 | 99.02         | -5.14 | 1.72      | -6.86     | 0.249              | -0.021             | -0.050             | 0.023              | 8.837       |
| 104 | 158 | 102.04        | -5.20 | 1.83      | -7.03     | 0.247              | -0.032             | -0.046             | 0.027              | 8.245       |
| 104 | 160 | 105.41        | -5.39 | 1.65      | -7.04     | 0.239              | -0.042             | -0.036             | 0.025              | 7.646       |
| 104 | 162 | 109.11        | -5.74 | 1.65      | -7.39     | 0.231              | -0.054             | -0.025             | 0.023              | 7.047       |
| 104 | 164 | 114.37        | -5.01 | 1.44      | -6.45     | 0.221              | -0.056             | -0.017             | 0.017              | 7.754       |
| 104 | 166 | 120.06        | -4.30 | 1.26      | -5.55     | 0.203              | -0.056             | -0.010             | 0.012              | 7.489       |
| 104 | 168 | 126.07        | -3.73 | 1.20      | -4.93     | 0.191              | -0.058             | -0.001             | 0.008              | 7.143       |
| 104 | 170 | 132.17        | -3.51 | 0.90      | -4.41     | 0.164              | -0.051             | 0.001              | 0.005              | 6.616       |
| 104 | 172 | 138.39        | -3.62 | 0.78      | -4.40     | 0.140              | -0.049             | 0.006              | 0.002              | 6.094       |
| 104 | 174 | 144.81        | -3.95 | 0.27      | -4.22     | -0.125             | 0.005              | 0.008              | -0.004             | 5.696       |
| 104 | 176 | 151.47        | -4.46 | 0.21      | -4.66     | -0.113             | -0.005             | 0.004              | 0.000              | 5.367       |
| 104 | 178 | 158.47        | -5.04 | 0.32      | -5.36     | -0.099             | -0.020             | 0.012              | 0.008              | 4.930       |
| 104 | 180 | 166.31        | -5.19 | 0.11      | -5.29     | -0.054             | -0.015             | -0.001             | 0.000              | 5.141       |
| 104 | 182 | 174.27        | -5.61 | 0.19      | -5.80     | -0.042             | -0.024             | -0.008             | -0.001             | 4.657       |
| 104 | 184 | 182.62        | -6.03 | 0.06      | -6.09     | -0.001             | 0.000              | 0.000              | 0.000              | 4.417       |
| 104 | 186 | 192.88        | -4.93 | 0.55      | -5.48     | -0.002             | 0.000              | 0.000              | -0.001             | 5.724       |
| 104 | 188 | 203.40        | -3.94 | 1.00      | -4.93     | 0.009              | 0.007              | 0.000              | -0.001             | 5.286       |
| 104 | 190 | 214.05        | -3.19 | 1.63      | -4.81     | 0.035              | 0.021              | -0.001             | -0.002             | 4.723       |
| 104 | 192 | 224.82        | -2.67 | 2.18      | -4.86     | 0.054              | 0.028              | -0.004             | -0.003             | 4.254       |
| 106 | 142 | 111.78        | -0.96 | 0.44      | -1.39     | 0.241              | 0.018              | -0.026             | -0.004             | 11.407      |
| 106 | 144 | 109.50        | -1.72 | 0.53      | -2.25     | 0.240              | 0.015              | -0.030             | -0.003             | 11.184      |
| 106 | 146 | 107.75        | -2.55 | 0.69      | -3.24     | 0.243              | 0.009              | -0.036             | 0.000              | 10.866      |
| 106 | 148 | 106.49        | -3.44 | 0.84      | -4.28     | 0.245              | 0.001              | -0.040             | 0.005              | 10.444      |
| 106 | 150 | 105.73        | -4.39 | 1.07      | -5.46     | 0.247              | -0.006             | -0.045             | 0.010              | 9.965       |
| 106 | 152 | 105.58        | -5.26 | 1.32      | -6.58     | 0.248              | -0.011             | -0.050             | 0.013              | 9.615       |
| 106 | 154 | 106.68        | -5.43 | 1.51      | -6.94     | 0.248              | -0.022             | -0.049             | 0.020              | 9.955       |
| 106 | 156 | 108.33        | -5.56 | 1.79      | -7.36     | 0.249              | -0.032             | -0.048             | 0.027              | 9.495       |
| 106 | 158 | 110.38        | -5.80 | 1.95      | -7.75     | 0.246              | -0.042             | -0.045             | 0.031              | 8.930       |
| 106 | 160 | 112.88        | -6.08 | 1.87      | -7.95     | 0.240              | -0.051             | -0.036             | 0.029              | 8.423       |
| 106 | 162 | 115.72        | -6.52 | 1.84      | -8.36     | 0.233              | -0.061             | -0.025             | 0.026              | 7.886       |
| 106 | 164 | 120.27        | -5.73 | 1.63      | -7.36     | 0.223              | -0.064             | -0.016             | 0.019              | 8.734       |
| 106 | 166 | 125.29        | -4.93 | 1.57      | -6.50     | 0.213              | -0.067             | -0.008             | 0.015              | 8.501       |
| 106 | 168 | 130.62        | -4.29 | 1.50      | -5.78     | 0.198              | -0.069             | 0.001              | 0.010              | 8.135       |
| 106 | 170 | 136.14        | -3.91 | 1.16      | -5.08     | 0.172              | -0.061             | 0.004              | 0.006              | 7.646       |
| 106 | 172 | 141.67        | -3.96 | 0.82      | -4.78     | 0.139              | -0.052             | 0.006              | 0.003              | 7.075       |
| 106 | 174 | 147.39        | -4.26 | 0.49      | -4.76     | 0.108              | -0.039             | 0.005              | 0.001              | 6.570       |

Continued. . .

Table 1 contd. . .

| Z   | N   | $M_{gs}^{th}$ | E     | $E_{mac}$ | $E_{mic}$ | $\beta_{20}^{min}$ | $\beta_{40}^{min}$ | $\beta_{60}^{min}$ | $\beta_{80}^{min}$ | $Q_{alpha}$ |
|-----|-----|---------------|-------|-----------|-----------|--------------------|--------------------|--------------------|--------------------|-------------|
| 106 | 176 | 153.46        | -4.63 | 0.62      | -5.25     | 0.095              | -0.045             | 0.011              | 0.000              | 6.227       |
| 106 | 178 | 159.84        | -5.12 | 0.31      | -5.43     | -0.098             | -0.021             | 0.012              | 0.008              | 5.944       |
| 106 | 180 | 166.98        | -5.25 | 0.10      | -5.35     | -0.052             | -0.016             | -0.002             | 0.000              | 6.087       |
| 106 | 182 | 174.32        | -5.58 | 0.01      | -5.59     | 0.000              | 0.000              | 0.000              | 0.000              | 5.589       |
| 106 | 184 | 182.03        | -5.94 | 0.02      | -5.95     | 0.000              | 0.000              | 0.000              | 0.000              | 5.338       |
| 106 | 186 | 191.61        | -4.82 | 0.38      | -5.20     | -0.001             | 0.001              | 0.001              | 0.000              | 6.571       |
| 106 | 188 | 201.50        | -3.77 | 0.84      | -4.60     | -0.003             | 0.008              | -0.002             | 0.001              | 6.200       |
| 106 | 190 | 211.58        | -2.90 | 1.43      | -4.33     | 0.022              | 0.014              | -0.003             | -0.001             | 5.757       |
| 106 | 192 | 221.70        | -2.37 | 2.14      | -4.51     | 0.050              | 0.027              | -0.005             | -0.002             | 5.225       |
| 108 | 144 | 126.16        | -1.31 | 0.40      | -1.71     | 0.243              | -0.013             | -0.026             | 0.001              | 11.960      |
| 108 | 146 | 123.55        | -2.17 | 0.49      | -2.66     | 0.240              | -0.012             | -0.029             | 0.006              | 11.621      |
| 108 | 148 | 121.44        | -3.09 | 0.60      | -3.69     | 0.240              | -0.014             | -0.032             | 0.008              | 11.266      |
| 108 | 150 | 119.83        | -4.08 | 0.86      | -4.94     | 0.242              | -0.021             | -0.037             | 0.012              | 10.914      |
| 108 | 152 | 118.87        | -4.97 | 1.00      | -5.97     | 0.242              | -0.022             | -0.041             | 0.013              | 10.715      |
| 108 | 154 | 119.00        | -5.30 | 1.24      | -6.53     | 0.243              | -0.034             | -0.039             | 0.020              | 10.994      |
| 108 | 156 | 119.69        | -5.60 | 1.53      | -7.13     | 0.243              | -0.044             | -0.037             | 0.027              | 10.581      |
| 108 | 158 | 120.79        | -6.00 | 1.82      | -7.83     | 0.242              | -0.053             | -0.037             | 0.030              | 10.039      |
| 108 | 160 | 122.30        | -6.50 | 1.87      | -8.37     | 0.238              | -0.062             | -0.027             | 0.029              | 9.501       |
| 108 | 162 | 124.18        | -7.13 | 2.03      | -9.17     | 0.233              | -0.071             | -0.021             | 0.029              | 8.869       |
| 108 | 164 | 127.94        | -6.36 | 1.88      | -8.24     | 0.225              | -0.074             | -0.013             | 0.023              | 9.795       |
| 108 | 166 | 132.25        | -5.52 | 1.83      | -7.35     | 0.218              | -0.076             | -0.005             | 0.019              | 9.554       |
| 108 | 168 | 136.91        | -4.80 | 1.80      | -6.60     | 0.205              | -0.079             | 0.003              | 0.012              | 9.193       |
| 108 | 170 | 141.81        | -4.29 | 1.50      | -5.79     | 0.180              | -0.072             | 0.008              | 0.007              | 8.765       |
| 108 | 172 | 146.58        | -4.37 | 0.75      | -5.12     | 0.133              | -0.051             | 0.006              | 0.003              | 8.013       |
| 108 | 174 | 151.54        | -4.69 | 0.58      | -5.27     | 0.106              | -0.045             | 0.006              | 0.001              | 7.445       |
| 108 | 176 | 156.89        | -5.06 | 0.70      | -5.76     | 0.096              | -0.049             | 0.013              | 0.000              | 7.078       |
| 108 | 178 | 162.79        | -5.30 | 0.26      | -5.56     | -0.094             | -0.019             | 0.011              | 0.006              | 6.905       |
| 108 | 180 | 169.18        | -5.47 | 0.09      | -5.56     | -0.046             | -0.015             | -0.002             | 0.000              | 6.915       |
| 108 | 182 | 175.85        | -5.76 | 0.01      | -5.78     | 0.000              | -0.001             | 0.000              | 0.000              | 6.446       |
| 108 | 184 | 182.95        | -6.04 | 0.01      | -6.05     | 0.000              | 0.000              | 0.000              | 0.000              | 6.203       |
| 108 | 186 | 191.89        | -4.86 | 0.10      | -4.97     | -0.002             | 0.000              | 0.000              | 0.000              | 7.427       |
| 108 | 188 | 201.18        | -3.72 | 0.53      | -4.25     | -0.002             | 0.001              | -0.001             | 0.000              | 7.143       |
| 108 | 190 | 210.70        | -2.74 | 1.00      | -3.74     | 0.007              | 0.009              | -0.002             | -0.001             | 6.766       |
| 108 | 192 | 220.20        | -2.14 | 2.11      | -4.25     | 0.046              | 0.026              | -0.005             | -0.002             | 6.191       |
| 110 | 146 | 141.58        | -1.19 | 0.21      | -1.41     | 0.220              | 0.008              | -0.026             | 0.001              | 12.994      |
| 110 | 148 | 138.71        | -2.06 | 0.32      | -2.39     | 0.228              | -0.002             | -0.029             | 0.005              | 12.735      |
| 110 | 150 | 136.32        | -3.02 | 0.47      | -3.49     | 0.235              | -0.009             | -0.033             | 0.008              | 12.458      |
| 110 | 152 | 134.55        | -3.91 | 0.71      | -4.63     | 0.239              | -0.016             | -0.038             | 0.011              | 12.293      |
| 110 | 154 | 133.94        | -4.19 | 0.88      | -5.06     | 0.236              | -0.031             | -0.034             | 0.016              | 12.648      |
| 110 | 156 | 133.83        | -4.50 | 1.12      | -5.62     | 0.234              | -0.044             | -0.030             | 0.021              | 12.405      |
| 110 | 158 | 134.05        | -5.01 | 1.37      | -6.38     | 0.232              | -0.057             | -0.024             | 0.023              | 11.935      |
| 110 | 160 | 134.59        | -5.71 | 1.60      | -7.31     | 0.228              | -0.067             | -0.017             | 0.023              | 11.369      |
| 110 | 162 | 135.47        | -6.56 | 1.91      | -8.47     | 0.226              | -0.077             | -0.012             | 0.025              | 10.741      |
| 110 | 164 | 138.18        | -6.09 | 1.91      | -7.99     | 0.217              | -0.081             | -0.002             | 0.019              | 11.573      |
| 110 | 166 | 141.49        | -5.49 | 1.99      | -7.48     | 0.211              | -0.084             | 0.006              | 0.015              | 11.123      |
| 110 | 168 | 145.22        | -4.95 | 2.14      | -7.08     | 0.202              | -0.089             | 0.013              | 0.009              | 10.546      |
| 110 | 170 | 149.23        | -4.58 | 0.78      | -5.36     | 0.147              | -0.052             | 0.001              | 0.006              | 9.896       |
| 110 | 172 | 153.13        | -4.80 | 0.67      | -5.47     | 0.127              | -0.049             | 0.006              | 0.003              | 8.886       |
| 110 | 174 | 157.33        | -5.15 | 0.55      | -5.70     | 0.095              | -0.045             | 0.007              | 0.001              | 8.329       |
| 110 | 176 | 161.96        | -5.51 | 0.72      | -6.23     | 0.093              | -0.050             | 0.015              | 0.000              | 7.990       |
| 110 | 178 | 167.29        | -5.60 | 0.18      | -5.78     | -0.085             | -0.015             | 0.010              | 0.005              | 7.978       |
| 110 | 180 | 172.88        | -5.86 | 0.07      | -5.92     | -0.037             | -0.013             | -0.002             | 0.000              | 7.670       |
| 110 | 182 | 178.88        | -6.13 | 0.01      | -6.14     | -0.002             | 0.002              | 0.001              | 0.000              | 7.273       |
| 110 | 184 | 185.35        | -6.32 | 0.02      | -6.34     | -0.002             | 0.001              | 0.000              | 0.000              | 7.076       |
| 110 | 186 | 193.58        | -5.16 | 0.01      | -5.18     | -0.001             | 0.000              | 0.000              | 0.001              | 8.204       |
| 110 | 188 | 202.31        | -3.89 | 0.02      | -3.91     | 0.000              | 0.000              | 0.000              | 0.000              | 7.998       |
| 110 | 190 | 211.29        | -2.76 | 0.45      | -3.22     | -0.002             | 0.002              | -0.001             | 0.000              | 7.681       |
| 110 | 192 | 220.27        | -2.00 | 1.99      | -4.00     | 0.045              | 0.024              | -0.005             | -0.002             | 7.156       |
| 112 | 148 | 157.46        | -1.17 | 0.12      | -1.28     | 0.211              | 0.005              | -0.025             | 0.002              | 13.458      |
| 112 | 150 | 154.38        | -2.01 | 0.23      | -2.24     | 0.223              | -0.003             | -0.029             | 0.006              | 13.246      |
| 112 | 152 | 151.87        | -2.85 | 0.42      | -3.27     | 0.233              | -0.010             | -0.034             | 0.009              | 13.121      |
| 112 | 154 | 150.48        | -3.11 | 0.53      | -3.64     | 0.222              | -0.028             | -0.028             | 0.012              | 13.506      |
| 112 | 156 | 149.51        | -3.50 | 0.75      | -4.25     | 0.218              | -0.044             | -0.022             | 0.014              | 13.136      |
| 112 | 158 | 148.83        | -4.12 | 1.05      | -5.16     | 0.217              | -0.058             | -0.014             | 0.016              | 12.576      |
| 112 | 160 | 148.46        | -4.95 | 1.46      | -6.41     | 0.218              | -0.071             | -0.008             | 0.020              | 11.987      |
| 112 | 162 | 148.45        | -5.93 | 1.95      | -7.89     | 0.221              | -0.083             | -0.004             | 0.024              | 11.441      |
| 112 | 164 | 150.12        | -5.74 | 1.98      | -7.72     | 0.208              | -0.087             | 0.003              | 0.016              | 12.224      |

Continued. . .

Table 1 contd. . .

| Z   | N   | $M_{gs}^{th}$ | E     | $E_{mac}$ | $E_{mic}$ | $\beta_{20}^{min}$ | $\beta_{40}^{min}$ | $\beta_{60}^{min}$ | $\beta_{80}^{min}$ | $Q_{alpha}$ |
|-----|-----|---------------|-------|-----------|-----------|--------------------|--------------------|--------------------|--------------------|-------------|
| 112 | 166 | 152.46        | -5.36 | 2.30      | -7.65     | 0.204              | -0.093             | 0.015              | 0.013              | 11.860      |
| 112 | 168 | 155.27        | -4.98 | 2.43      | -7.42     | 0.193              | -0.095             | 0.021              | 0.009              | 11.356      |
| 112 | 170 | 158.33        | -4.84 | 0.87      | -5.71     | 0.145              | -0.057             | 0.006              | 0.005              | 10.684      |
| 112 | 172 | 161.43        | -5.11 | 0.84      | -5.95     | 0.129              | -0.056             | 0.011              | 0.003              | 9.774       |
| 112 | 174 | 164.87        | -5.49 | 0.56      | -6.05     | 0.094              | -0.045             | 0.010              | 0.001              | 9.324       |
| 112 | 176 | 168.80        | -5.84 | 0.77      | -6.61     | 0.089              | -0.052             | 0.016              | -0.001             | 9.042       |
| 112 | 178 | 173.31        | -6.03 | 0.10      | -6.13     | -0.073             | -0.009             | 0.008              | 0.003              | 8.928       |
| 112 | 180 | 178.07        | -6.41 | 0.01      | -6.42     | 0.004              | -0.002             | 0.000              | 0.000              | 8.357       |
| 112 | 182 | 183.38        | -6.65 | 0.01      | -6.67     | 0.000              | 0.000              | 0.001              | 0.000              | 8.074       |
| 112 | 184 | 189.26        | -6.74 | 0.01      | -6.75     | 0.000              | 0.000              | 0.000              | 0.000              | 7.964       |
| 112 | 186 | 196.82        | -5.56 | 0.01      | -5.57     | -0.001             | 0.000              | 0.000              | 0.000              | 9.040       |
| 112 | 188 | 204.87        | -4.29 | 0.01      | -4.30     | 0.000              | 0.002              | 0.001              | 0.000              | 8.864       |
| 112 | 190 | 213.23        | -3.09 | 0.01      | -3.11     | 0.000              | 0.000              | 0.000              | 0.000              | 8.493       |
| 112 | 192 | 221.86        | -2.01 | 0.01      | -2.02     | 0.000              | 0.000              | 0.000              | 0.000              | 8.147       |
| 114 | 150 | 173.88        | -1.15 | -0.06     | -1.08     | 0.231              | 0.008              | -0.023             | 0.007              | 13.996      |
| 114 | 152 | 170.63        | -1.93 | 0.11      | -2.04     | 0.237              | -0.002             | -0.029             | 0.009              | 13.828      |
| 114 | 154 | 168.45        | -2.20 | 0.27      | -2.47     | 0.212              | -0.027             | -0.021             | 0.008              | 14.153      |
| 114 | 156 | 166.58        | -2.70 | 0.51      | -3.20     | 0.200              | -0.044             | -0.012             | 0.010              | 13.675      |
| 114 | 158 | 165.05        | -3.40 | 0.84      | -4.24     | 0.201              | -0.058             | -0.005             | 0.012              | 13.116      |
| 114 | 160 | 163.81        | -4.33 | 1.35      | -5.68     | 0.206              | -0.073             | -0.001             | 0.017              | 12.555      |
| 114 | 162 | 163.01        | -5.34 | 1.98      | -7.31     | 0.213              | -0.087             | 0.002              | 0.023              | 12.127      |
| 114 | 164 | 163.65        | -5.41 | 2.13      | -7.55     | 0.202              | -0.091             | 0.012              | 0.017              | 12.771      |
| 114 | 166 | 165.08        | -5.20 | 2.48      | -7.68     | 0.196              | -0.098             | 0.021              | 0.013              | 12.532      |
| 114 | 168 | 166.96        | -5.00 | 2.93      | -7.93     | 0.191              | -0.104             | 0.031              | 0.009              | 12.078      |
| 114 | 170 | 169.24        | -4.90 | 1.43      | -6.33     | 0.151              | -0.073             | 0.018              | 0.005              | 11.544      |
| 114 | 172 | 171.55        | -5.23 | 0.22      | -5.45     | -0.120             | 0.023              | 0.003              | -0.008             | 10.798      |
| 114 | 174 | 174.18        | -5.70 | 0.37      | -6.06     | 0.086              | -0.037             | 0.008              | 0.001              | 10.321      |
| 114 | 176 | 177.37        | -6.06 | 0.05      | -6.11     | -0.074             | -0.002             | 0.005              | 0.001              | 10.070      |
| 114 | 178 | 180.60        | -6.82 | 0.01      | -6.83     | 0.000              | 0.000              | 0.000              | 0.000              | 9.608       |
| 114 | 180 | 184.90        | -6.94 | 0.01      | -6.95     | 0.001              | 0.000              | 0.000              | 0.000              | 9.167       |
| 114 | 182 | 189.61        | -7.09 | 0.01      | -7.10     | 0.000              | 0.000              | 0.000              | 0.000              | 9.113       |
| 114 | 184 | 194.90        | -7.07 | 0.01      | -7.09     | 0.000              | 0.000              | 0.000              | 0.000              | 9.088       |
| 114 | 186 | 201.76        | -5.90 | 0.01      | -5.91     | -0.001             | 0.001              | 0.001              | 0.000              | 10.067      |
| 114 | 188 | 209.12        | -4.62 | 0.01      | -4.63     | 0.000              | 0.000              | 0.000              | 0.000              | 9.878       |
| 114 | 190 | 216.80        | -3.42 | 0.01      | -3.43     | 0.000              | 0.000              | 0.000              | 0.000              | 9.511       |
| 114 | 192 | 224.76        | -2.34 | 0.01      | -2.35     | 0.000              | 0.001              | 0.000              | 0.000              | 9.109       |
| 116 | 152 | 190.84        | -1.14 | -0.14     | -1.00     | 0.240              | 0.004              | -0.026             | 0.008              | 14.533      |
| 116 | 154 | 187.96        | -1.32 | 0.03      | -1.35     | 0.213              | -0.024             | -0.015             | 0.008              | 14.900      |
| 116 | 156 | 185.22        | -1.91 | 0.49      | -2.41     | 0.192              | -0.051             | -0.002             | 0.007              | 14.346      |
| 116 | 158 | 182.78        | -2.75 | 0.97      | -3.72     | 0.192              | -0.066             | 0.004              | 0.011              | 13.769      |
| 116 | 160 | 180.71        | -3.74 | 1.45      | -5.18     | 0.196              | -0.078             | 0.007              | 0.017              | 13.243      |
| 116 | 162 | 179.14        | -4.76 | 1.99      | -6.75     | 0.204              | -0.089             | 0.006              | 0.024              | 12.900      |
| 116 | 164 | 178.77        | -5.08 | 2.20      | -7.28     | 0.192              | -0.094             | 0.017              | 0.016              | 13.336      |
| 116 | 166 | 179.28        | -5.04 | 2.60      | -7.63     | 0.186              | -0.100             | 0.027              | 0.013              | 13.207      |
| 116 | 168 | 180.28        | -4.99 | 3.03      | -8.01     | 0.181              | -0.105             | 0.035              | 0.009              | 12.783      |
| 116 | 170 | 181.70        | -5.01 | 0.11      | -5.11     | -0.111             | 0.017              | 0.002              | -0.004             | 12.307      |
| 116 | 172 | 183.07        | -5.55 | 0.14      | -5.68     | -0.115             | 0.018              | 0.005              | -0.007             | 11.401      |
| 116 | 174 | 185.12        | -5.87 | 0.05      | -5.92     | -0.092             | 0.005              | 0.004              | -0.002             | 11.140      |
| 116 | 176 | 187.52        | -6.29 | 0.05      | -6.34     | -0.078             | -0.004             | 0.006              | 0.000              | 10.920      |
| 116 | 178 | 190.43        | -6.67 | 0.09      | -6.76     | -0.075             | -0.009             | 0.010              | 0.003              | 10.632      |
| 116 | 180 | 193.97        | -6.85 | 0.01      | -6.86     | 0.002              | 0.000              | 0.000              | 0.000              | 10.712      |
| 116 | 182 | 198.03        | -6.94 | 0.01      | -6.95     | 0.001              | 0.000              | 0.000              | 0.000              | 10.703      |
| 116 | 184 | 202.68        | -6.86 | 0.01      | -6.87     | -0.001             | 0.000              | 0.000              | 0.000              | 10.647      |
| 116 | 186 | 208.82        | -5.71 | 0.01      | -5.73     | 0.000              | 0.001              | 0.000              | 0.000              | 11.498      |
| 116 | 188 | 215.48        | -4.46 | 0.01      | -4.47     | 0.000              | 0.000              | 0.000              | 0.000              | 11.296      |
| 116 | 190 | 222.46        | -3.28 | 0.01      | -3.29     | 0.000              | 0.001              | 0.000              | 0.000              | 10.910      |
| 116 | 192 | 229.72        | -2.22 | 0.01      | -2.23     | 0.000              | 0.000              | 0.000              | 0.000              | 10.489      |
| 118 | 154 | 208.87        | -0.60 | -0.23     | -0.37     | 0.219              | -0.018             | -0.011             | 0.008              | 15.605      |
| 118 | 156 | 205.37        | -1.17 | 0.41      | -1.58     | 0.177              | -0.050             | 0.004              | 0.006              | 14.990      |
| 118 | 158 | 202.18        | -1.99 | 0.75      | -2.74     | 0.182              | -0.061             | 0.007              | 0.009              | 14.537      |
| 118 | 160 | 199.43        | -2.90 | 1.07      | -3.97     | 0.190              | -0.071             | 0.007              | 0.013              | 14.229      |
| 118 | 162 | 197.15        | -3.87 | 1.64      | -5.50     | 0.203              | -0.083             | 0.007              | 0.022              | 14.013      |
| 118 | 164 | 195.98        | -4.24 | 1.84      | -6.08     | 0.186              | -0.087             | 0.017              | 0.015              | 14.415      |
| 118 | 166 | 195.72        | -4.22 | 2.11      | -6.33     | 0.175              | -0.091             | 0.025              | 0.010              | 14.518      |
| 118 | 168 | 195.78        | -4.37 | 0.03      | -4.40     | -0.107             | 0.009              | 0.004              | -0.002             | 14.072      |
| 118 | 170 | 195.79        | -5.06 | 0.06      | -5.12     | -0.116             | 0.012              | 0.006              | -0.004             | 13.078      |
| 118 | 172 | 196.46        | -5.57 | 0.11      | -5.68     | -0.122             | 0.015              | 0.008              | -0.006             | 12.335      |

Continued. . .

Table 1 contd. . .

| Z   | N   | $M_{gs}^{th}$ | E     | $E_{mac}$ | $E_{mic}$ | $\beta_{20}^{min}$ | $\beta_{40}^{min}$ | $\beta_{60}^{min}$ | $\beta_{80}^{min}$ | $Q_{alpha}$ |
|-----|-----|---------------|-------|-----------|-----------|--------------------|--------------------|--------------------|--------------------|-------------|
| 118 | 174 | 197.76        | -5.91 | 0.38      | -6.29     | 0.081              | -0.038             | 0.011              | 0.001              | 12.270      |
| 118 | 176 | 199.63        | -6.16 | 0.06      | -6.23     | -0.090             | -0.008             | 0.008              | 0.002              | 12.088      |
| 118 | 178 | 201.86        | -6.49 | 0.15      | -6.64     | -0.087             | -0.014             | 0.012              | 0.005              | 11.915      |
| 118 | 180 | 204.92        | -6.45 | 0.06      | -6.50     | -0.037             | -0.013             | -0.002             | 0.000              | 12.069      |
| 118 | 182 | 208.38        | -6.44 | 0.01      | -6.45     | 0.000              | 0.000              | 0.000              | 0.000              | 11.983      |
| 118 | 184 | 212.40        | -6.29 | 0.01      | -6.31     | 0.000              | 0.000              | 0.000              | 0.000              | 11.949      |
| 118 | 186 | 217.82        | -5.19 | 0.01      | -5.20     | -0.001             | 0.000              | 0.000              | 0.000              | 12.707      |
| 118 | 188 | 223.76        | -3.96 | 0.01      | -3.97     | 0.000              | -0.001             | 0.000              | 0.000              | 12.519      |
| 118 | 190 | 230.04        | -2.81 | 0.01      | -2.82     | -0.001             | 0.000              | 0.000              | 0.000              | 12.134      |
| 118 | 192 | 236.11        | -2.26 | 1.32      | -3.58     | -0.404             | 0.006              | 0.010              | -0.010             | 11.224      |
| 120 | 156 | 225.79        | -1.71 | 0.41      | -2.12     | -0.432             | 0.036              | 0.015              | -0.015             | 14.491      |
| 120 | 158 | 222.21        | -2.14 | 0.53      | -2.68     | -0.435             | 0.039              | 0.016              | -0.016             | 14.408      |
| 120 | 160 | 219.14        | -2.61 | 0.65      | -3.27     | -0.439             | 0.043              | 0.016              | -0.016             | 14.532      |
| 120 | 162 | 216.58        | -3.10 | 0.77      | -3.87     | -0.442             | 0.048              | 0.016              | -0.016             | 14.729      |
| 120 | 164 | 214.62        | -3.51 | 0.89      | -4.40     | -0.444             | 0.052              | 0.016              | -0.016             | 15.047      |
| 120 | 166 | 213.60        | -3.51 | 1.03      | -4.53     | -0.451             | 0.055              | 0.016              | -0.017             | 15.195      |
| 120 | 168 | 212.38        | -4.20 | 0.02      | -4.22     | -0.123             | 0.012              | 0.008              | -0.001             | 14.239      |
| 120 | 170 | 211.64        | -4.91 | 0.05      | -4.96     | -0.130             | 0.013              | 0.010              | -0.003             | 13.437      |
| 120 | 172 | 211.58        | -5.41 | 0.11      | -5.53     | -0.136             | 0.016              | 0.013              | -0.007             | 13.372      |
| 120 | 174 | 212.27        | -5.66 | 0.60      | -6.25     | 0.084              | -0.047             | 0.016              | 0.003              | 13.390      |
| 120 | 176 | 213.43        | -5.89 | 0.92      | -6.81     | 0.085              | -0.056             | 0.023              | 0.003              | 13.241      |
| 120 | 178 | 215.19        | -5.99 | 0.14      | -6.12     | -0.092             | -0.013             | 0.014              | 0.005              | 13.138      |
| 120 | 180 | 217.64        | -5.85 | 0.09      | -5.94     | -0.036             | -0.018             | -0.004             | 0.000              | 13.347      |
| 120 | 182 | 220.46        | -5.78 | 0.01      | -5.79     | 0.000              | 0.000              | 0.000              | 0.000              | 13.114      |
| 120 | 184 | 223.87        | -5.56 | 0.01      | -5.57     | 0.000              | 0.000              | 0.000              | 0.000              | 13.069      |
| 120 | 186 | 228.56        | -4.48 | 0.01      | -4.49     | 0.000              | 0.000              | 0.000              | 0.000              | 13.730      |
| 120 | 188 | 233.81        | -3.26 | 0.39      | -3.65     | 0.016              | 0.005              | 0.004              | 0.001              | 13.570      |
| 120 | 190 | 238.78        | -2.74 | 1.08      | -3.82     | -0.407             | 0.006              | 0.013              | -0.012             | 12.592      |
| 120 | 192 | 243.80        | -2.58 | 1.10      | -3.68     | -0.413             | 0.009              | 0.010              | -0.011             | 11.334      |
| 122 | 158 | 244.04        | -2.01 | 0.06      | -2.07     | -0.446             | 0.044              | 0.009              | -0.016             | 15.830      |
| 122 | 160 | 240.10        | -2.60 | 0.19      | -2.79     | -0.449             | 0.047              | 0.010              | -0.016             | 15.463      |
| 122 | 162 | 236.67        | -3.20 | 0.32      | -3.52     | -0.452             | 0.052              | 0.011              | -0.016             | 15.109      |
| 122 | 164 | 233.85        | -3.73 | 0.45      | -4.18     | -0.456             | 0.056              | 0.011              | -0.016             | 14.845      |
| 122 | 166 | 231.92        | -3.88 | 0.61      | -4.49     | -0.464             | 0.059              | 0.012              | -0.017             | 14.873      |
| 122 | 168 | 230.59        | -3.95 | 0.00      | -3.95     | -0.143             | 0.016              | 0.009              | 0.000              | 14.566      |
| 122 | 170 | 229.10        | -4.68 | 0.03      | -4.71     | -0.145             | 0.015              | 0.013              | -0.003             | 14.292      |
| 122 | 172 | 228.30        | -5.21 | 0.11      | -5.31     | -0.147             | 0.016              | 0.016              | -0.006             | 14.233      |
| 122 | 174 | 228.52        | -5.19 | 0.05      | -5.25     | -0.135             | 0.009              | 0.015              | -0.002             | 14.512      |
| 122 | 176 | 229.19        | -5.21 | 0.04      | -5.25     | -0.116             | -0.003             | 0.013              | 0.002              | 14.494      |
| 122 | 178 | 230.26        | -5.29 | 0.17      | -5.46     | -0.104             | -0.017             | 0.014              | 0.007              | 14.402      |
| 122 | 180 | 232.09        | -5.06 | 0.14      | -5.20     | -0.038             | -0.022             | -0.006             | 0.000              | 14.478      |
| 122 | 182 | 234.28        | -4.93 | 0.01      | -4.94     | 0.000              | 0.000              | 0.000              | 0.000              | 14.218      |
| 122 | 184 | 237.06        | -4.64 | 0.01      | -4.65     | 0.000              | 0.000              | 0.000              | 0.000              | 14.171      |
| 122 | 186 | 240.99        | -3.64 | 0.63      | -4.27     | 0.014              | 0.003              | 0.013              | 0.002              | 14.696      |
| 122 | 188 | 244.94        | -3.04 | 0.15      | -3.18     | -0.189             | -0.001             | 0.017              | 0.007              | 13.958      |
| 122 | 190 | 249.04        | -2.71 | 0.23      | -2.94     | -0.199             | -0.006             | 0.020              | 0.008              | 12.808      |
| 122 | 192 | 253.50        | -2.43 | 0.79      | -3.22     | -0.420             | 0.010              | 0.007              | -0.010             | 12.296      |
| 124 | 160 | 262.80        | -2.34 | -0.33     | -2.02     | -0.459             | 0.050              | 0.007              | -0.014             | 16.330      |
| 124 | 162 | 258.56        | -3.01 | -0.19     | -2.81     | -0.462             | 0.054              | 0.008              | -0.015             | 16.043      |
| 124 | 164 | 254.92        | -3.62 | -0.05     | -3.56     | -0.465             | 0.057              | 0.009              | -0.016             | 15.820      |
| 124 | 166 | 252.10        | -3.92 | 0.10      | -4.02     | -0.473             | 0.061              | 0.010              | -0.016             | 15.825      |
| 124 | 168 | 250.51        | -3.51 | 0.20      | -3.71     | -0.477             | 0.064              | 0.006              | -0.016             | 16.163      |
| 124 | 170 | 248.31        | -4.22 | -0.04     | -4.19     | -0.163             | 0.019              | 0.012              | -0.001             | 15.293      |
| 124 | 172 | 246.78        | -4.75 | 0.04      | -4.79     | -0.163             | 0.017              | 0.017              | -0.005             | 15.256      |
| 124 | 174 | 246.39        | -4.64 | 0.02      | -4.66     | -0.167             | 0.017              | 0.017              | -0.002             | 15.663      |
| 124 | 176 | 246.37        | -4.63 | 0.15      | -4.78     | -0.211             | 0.042              | 0.010              | -0.004             | 15.421      |
| 124 | 178 | 246.52        | -4.92 | 0.30      | -5.22     | -0.230             | 0.050              | 0.011              | -0.007             | 14.901      |
| 124 | 180 | 247.70        | -4.65 | 0.32      | -4.97     | -0.241             | 0.048              | 0.015              | -0.008             | 15.017      |
| 124 | 182 | 249.62        | -4.08 | 0.27      | -4.35     | -0.241             | 0.043              | 0.017              | -0.007             | 15.101      |
| 124 | 184 | 251.77        | -3.73 | 1.57      | -5.30     | 0.018              | -0.001             | 0.029              | -0.012             | 15.067      |
| 124 | 186 | 254.45        | -3.30 | 0.04      | -3.34     | -0.194             | 0.007              | 0.016              | 0.009              | 14.966      |
| 124 | 188 | 257.40        | -3.02 | 0.13      | -3.15     | -0.200             | -0.002             | 0.020              | 0.010              | 13.984      |
| 124 | 190 | 260.75        | -2.77 | 0.22      | -2.98     | -0.205             | -0.007             | 0.023              | 0.010              | 13.382      |
| 124 | 192 | 264.52        | -2.51 | 0.37      | -2.87     | -0.212             | -0.015             | 0.025              | 0.013              | 13.053      |
| 126 | 162 | 281.99        | -2.77 | -0.75     | -2.02     | -0.471             | 0.056              | 0.005              | -0.013             | 16.762      |
| 126 | 164 | 277.54        | -3.44 | -0.61     | -2.83     | -0.474             | 0.060              | 0.006              | -0.013             | 16.547      |
| 126 | 166 | 273.85        | -3.88 | -0.45     | -3.42     | -0.482             | 0.064              | 0.008              | -0.015             | 16.507      |

Continued. . .

Table 1 contd. . .

| Z   | N   | $M_{gs}^{th}$ | E     | $E_{mac}$ | $E_{mic}$ | $\beta_{20}^{min}$ | $\beta_{40}^{min}$ | $\beta_{60}^{min}$ | $\beta_{80}^{min}$ | $Q_{alpha}$ |
|-----|-----|---------------|-------|-----------|-----------|--------------------|--------------------|--------------------|--------------------|-------------|
| 126 | 168 | 271.43        | -3.57 | -0.34     | -3.23     | -0.488             | 0.067              | 0.004              | -0.015             | 16.898      |
| 126 | 170 | 269.00        | -3.78 | -0.12     | -3.66     | -0.180             | 0.021              | 0.014              | 0.000              | 16.064      |
| 126 | 172 | 266.79        | -4.28 | -0.05     | -4.23     | -0.178             | 0.019              | 0.018              | -0.003             | 16.052      |
| 126 | 174 | 265.48        | -4.36 | -0.06     | -4.30     | -0.195             | 0.027              | 0.016              | -0.001             | 16.280      |
| 126 | 176 | 264.56        | -4.54 | -0.01     | -4.53     | -0.214             | 0.037              | 0.014              | -0.002             | 15.754      |
| 126 | 178 | 264.04        | -4.80 | 0.09      | -4.88     | -0.229             | 0.044              | 0.014              | -0.004             | 15.250      |
| 126 | 180 | 264.51        | -4.53 | 0.10      | -4.63     | -0.238             | 0.041              | 0.019              | -0.005             | 15.569      |
| 126 | 182 | 265.70        | -4.00 | 0.06      | -4.07     | -0.236             | 0.034              | 0.021              | -0.002             | 15.580      |
| 126 | 184 | 267.32        | -3.50 | -0.01     | -3.49     | -0.220             | 0.021              | 0.020              | 0.004              | 15.276      |
| 126 | 186 | 269.19        | -3.19 | 0.00      | -3.19     | -0.211             | 0.008              | 0.020              | 0.009              | 14.993      |
| 126 | 188 | 271.41        | -2.96 | 0.10      | -3.06     | -0.212             | -0.002             | 0.023              | 0.011              | 14.537      |
| 126 | 190 | 274.01        | -2.78 | 0.26      | -3.04     | -0.214             | -0.010             | 0.027              | 0.014              | 14.190      |
| 126 | 192 | 277.07        | -2.57 | 0.36      | -2.93     | -0.220             | -0.016             | 0.028              | 0.016              | 13.896      |

**Table 2. Saddle point properties**

For the isotopes of the elements  $Z=98-126$ , tabulates the saddle point masses, total energies, macroscopic and microscopic energies as well as saddle point deformations.

|  |                               |
|--|-------------------------------|
| $Z$                                    | The atomic number             |
| $A$                                    | The mass number               |
| $M_{sp}^{th}$                          | The mass excess in MeV        |
| $E$                                    | The total energy in MeV       |
| $E_{mac}$                              | The macroscopic energy in MeV |
| $E_{mic}$                              | The microscopic energy in MeV |
| $\beta_{20}^{sp} \div \beta_{80}^{sp}$ | The saddle point deformations |
| $Q_{alpha}$                            | Theoretical $Q$ -value in MeV |



**Table 1**

Calculated Saddle Point Masses and Deformations.

| Z   | N   | $M_{sp}^{th}$ | E     | $E_{mac}$ | $E_{mic}$ | $\beta_{20}^{sp}$ | $\gamma^{sp}(^\circ)$ | $\beta_{40}^{sp}$ | $\beta_{42}^{sp}$ | $\beta_{44}^{sp}$ | $\beta_{60}^{sp}$ | $\beta_{80}^{sp}$ |
|-----|-----|---------------|-------|-----------|-----------|-------------------|-----------------------|-------------------|-------------------|-------------------|-------------------|-------------------|
| 98  | 134 | 61.77         | 2.33  | 1.64      | 0.68      | 0.393             | 7.3                   | -0.010            | 0.009             | -0.003            | -0.014            | -0.019            |
| 98  | 136 | 61.12         | 2.12  | 2.18      | -0.06     | 0.412             | 5.6                   | -0.030            | 0.015             | 0.003             | -0.022            | -0.015            |
| 98  | 138 | 61.49         | 2.35  | 2.18      | 0.18      | 0.421             | 2.7                   | -0.030            | 0.008             | 0.003             | -0.026            | -0.008            |
| 98  | 140 | 62.69         | 2.82  | 2.23      | 0.59      | 0.440             | 0.0                   | -0.030            | 0.000             | -0.002            | -0.025            | 0.001             |
| 98  | 142 | 64.26         | 3.10  | 2.45      | 0.65      | 0.475             | 8.5                   | -0.010            | 0.017             | 0.022             | -0.011            | 0.001             |
| 98  | 144 | 66.18         | 3.15  | 2.55      | 0.61      | 0.510             | 11.3                  | 0.000             | 0.000             | 0.023             | 0.006             | -0.002            |
| 98  | 146 | 68.18         | 2.75  | 2.85      | -0.10     | 0.526             | 14.3                  | 0.030             | 0.002             | 0.025             | 0.020             | 0.005             |
| 98  | 148 | 70.79         | 2.43  | 2.91      | -0.48     | 0.526             | 14.3                  | 0.030             | 0.003             | 0.025             | 0.018             | 0.007             |
| 98  | 150 | 74.09         | 2.26  | 2.71      | -0.45     | 0.500             | 16.3                  | 0.030             | 0.004             | 0.019             | 0.003             | 0.011             |
| 98  | 152 | 77.80         | 2.00  | 2.65      | -0.66     | 0.490             | 16.6                  | 0.030             | 0.005             | 0.015             | 0.001             | 0.012             |
| 98  | 154 | 81.89         | 1.61  | 2.77      | -1.16     | 0.500             | 16.3                  | 0.040             | 0.007             | 0.014             | 0.006             | 0.012             |
| 98  | 156 | 86.41         | 1.17  | 2.77      | -1.60     | 0.517             | 14.6                  | 0.040             | 0.006             | 0.018             | 0.006             | 0.008             |
| 98  | 158 | 91.60         | 0.90  | 2.84      | -1.94     | 0.536             | 14.0                  | 0.040             | -0.001            | 0.021             | 0.003             | 0.003             |
| 98  | 160 | 97.28         | 0.66  | 2.99      | -2.33     | 0.573             | 12.1                  | 0.030             | -0.008            | 0.024             | -0.004            | -0.004            |
| 98  | 162 | 103.77        | 0.78  | 3.01      | -2.24     | 0.575             | 13.1                  | 0.030             | -0.005            | 0.018             | -0.009            | -0.004            |
| 98  | 164 | 110.67        | 0.85  | 2.91      | -2.06     | 0.582             | 11.9                  | 0.030             | -0.006            | 0.012             | -0.012            | -0.002            |
| 98  | 166 | 118.04        | 0.94  | 2.88      | -1.94     | 0.582             | 11.9                  | 0.030             | -0.006            | 0.007             | -0.013            | -0.001            |
| 98  | 168 | 125.77        | 0.97  | 2.82      | -1.86     | 0.590             | 10.7                  | 0.030             | -0.007            | 0.003             | -0.013            | 0.001             |
| 98  | 170 | 133.94        | 1.01  | 2.85      | -1.84     | 0.592             | 11.7                  | 0.040             | -0.005            | 0.002             | -0.015            | 0.003             |
| 98  | 172 | 141.21        | -0.27 | 1.10      | -1.37     | 0.280             | 0.0                   | 0.020             | 0.000             | 0.000             | 0.006             | 0.018             |
| 98  | 174 | 150.37        | -0.06 | 1.04      | -1.11     | 0.270             | 0.0                   | 0.020             | 0.000             | 0.000             | 0.013             | 0.014             |
| 98  | 176 | 159.70        | -0.09 | 1.32      | -1.41     | 0.297             | 19.7                  | 0.020             | -0.009            | -0.005            | 0.012             | 0.007             |
| 98  | 178 | 169.26        | -0.28 | 1.35      | -1.63     | 0.307             | 19.0                  | 0.020             | -0.007            | -0.006            | 0.013             | 0.004             |
| 98  | 180 | 179.14        | -0.53 | 1.46      | -1.99     | 0.320             | 20.1                  | 0.030             | -0.004            | -0.005            | 0.011             | 0.002             |
| 98  | 182 | 189.35        | -0.84 | 1.58      | -2.41     | 0.323             | 21.8                  | 0.040             | 0.001             | -0.001            | 0.010             | 0.000             |
| 98  | 184 | 199.83        | -1.24 | 1.51      | -2.74     | 0.345             | 16.9                  | 0.030             | -0.003            | -0.007            | 0.008             | -0.006            |
| 98  | 186 | 210.79        | -1.52 | 1.55      | -3.07     | 0.369             | 12.5                  | 0.010             | -0.007            | -0.007            | 0.004             | -0.012            |
| 98  | 188 | 222.04        | -1.88 | 1.11      | -2.99     | 0.199             | 40.9                  | 0.040             | -0.003            | -0.013            | 0.015             | 0.005             |
| 98  | 190 | 233.68        | -2.20 | 1.42      | -3.62     | 0.190             | 18.4                  | 0.060             | 0.005             | -0.002            | 0.029             | 0.002             |
| 98  | 192 | 245.59        | -2.58 | 1.60      | -4.18     | 0.197             | 14.7                  | 0.070             | 0.006             | -0.002            | 0.027             | -0.001            |
| 100 | 136 | 74.40         | 2.50  | 1.64      | 0.86      | 0.410             | 0.0                   | -0.030            | 0.000             | 0.000             | -0.019            | -0.014            |
| 100 | 138 | 73.91         | 2.73  | 1.71      | 1.02      | 0.420             | 0.0                   | -0.030            | 0.000             | 0.000             | -0.022            | -0.007            |
| 100 | 140 | 73.86         | 2.81  | 2.14      | 0.67      | 0.509             | 19.5                  | 0.060             | -0.016            | 0.007             | 0.009             | -0.003            |
| 100 | 142 | 74.33         | 2.84  | 2.48      | 0.35      | 0.488             | 22.9                  | 0.070             | -0.013            | 0.009             | 0.003             | -0.001            |
| 100 | 144 | 75.28         | 2.78  | 2.45      | 0.32      | 0.488             | 22.9                  | 0.060             | -0.014            | 0.008             | -0.001            | 0.002             |
| 100 | 146 | 76.80         | 2.73  | 2.26      | 0.47      | 0.490             | 20.3                  | 0.050             | -0.011            | 0.011             | -0.001            | 0.004             |
| 100 | 148 | 78.70         | 2.52  | 2.26      | 0.26      | 0.487             | 19.2                  | 0.050             | -0.001            | 0.013             | 0.002             | 0.008             |
| 100 | 150 | 81.04         | 2.22  | 2.22      | 0.00      | 0.484             | 18.1                  | 0.040             | 0.002             | 0.014             | 0.002             | 0.011             |
| 100 | 152 | 83.83         | 1.85  | 2.24      | -0.39     | 0.481             | 16.9                  | 0.050             | 0.004             | 0.012             | 0.005             | 0.013             |
| 100 | 154 | 87.06         | 1.41  | 2.34      | -0.93     | 0.481             | 16.9                  | 0.060             | 0.007             | 0.008             | 0.004             | 0.014             |
| 100 | 156 | 90.76         | 0.95  | 2.57      | -1.63     | 0.474             | 18.4                  | 0.070             | 0.011             | 0.004             | 0.001             | 0.014             |
| 100 | 158 | 95.01         | 0.54  | 2.61      | -2.07     | 0.430             | 17.6                  | 0.080             | 0.007             | -0.013            | -0.005            | 0.019             |
| 100 | 160 | 99.66         | 0.06  | 2.71      | -2.65     | 0.381             | 13.7                  | 0.090             | 0.004             | -0.023            | -0.010            | 0.021             |
| 100 | 162 | 105.43        | 0.22  | 2.50      | -2.28     | 0.592             | 11.7                  | 0.030             | -0.002            | 0.020             | -0.008            | -0.005            |
| 100 | 164 | 111.61        | 0.34  | 2.46      | -2.11     | 0.585             | 12.9                  | 0.040             | -0.001            | 0.015             | -0.009            | -0.003            |
| 100 | 166 | 118.17        | 0.40  | 2.37      | -1.97     | 0.592             | 11.7                  | 0.040             | -0.001            | 0.011             | -0.012            | -0.003            |
| 100 | 168 | 125.17        | 0.45  | 2.40      | -1.95     | 0.594             | 12.6                  | 0.050             | -0.001            | 0.007             | -0.012            | 0.000             |
| 100 | 170 | 132.57        | 0.47  | 2.32      | -1.85     | 0.602             | 11.5                  | 0.050             | -0.001            | 0.005             | -0.013            | 0.002             |
| 100 | 172 | 139.41        | -0.50 | 1.05      | -1.55     | 0.290             | 0.0                   | 0.020             | 0.000             | 0.000             | 0.004             | 0.020             |
| 100 | 174 | 147.86        | -0.27 | 0.98      | -1.24     | 0.280             | 0.0                   | 0.020             | 0.000             | 0.000             | 0.008             | 0.016             |
| 100 | 176 | 156.63        | -0.12 | 0.94      | -1.07     | 0.270             | 0.0                   | 0.020             | 0.000             | 0.000             | 0.016             | 0.012             |
| 100 | 178 | 165.64        | -0.13 | 1.03      | -1.16     | 0.270             | 0.0                   | 0.030             | 0.000             | 0.000             | 0.019             | 0.010             |
| 100 | 180 | 174.82        | -0.37 | 1.38      | -1.74     | 0.314             | 22.5                  | 0.030             | -0.007            | -0.005            | 0.014             | -0.001            |
| 100 | 182 | 184.27        | -0.73 | 1.41      | -2.14     | 0.318             | 24.2                  | 0.030             | -0.003            | -0.001            | 0.013             | -0.002            |
| 100 | 184 | 194.05        | -1.13 | 1.43      | -2.56     | 0.313             | 26.6                  | 0.030             | 0.001             | 0.001             | 0.012             | -0.004            |
| 100 | 186 | 204.27        | -1.45 | 1.38      | -2.84     | 0.361             | 14.4                  | 0.020             | -0.007            | -0.009            | 0.005             | -0.011            |
| 100 | 188 | 214.78        | -1.85 | 1.15      | -3.01     | 0.194             | 34.5                  | 0.050             | -0.003            | -0.008            | 0.017             | 0.005             |
| 100 | 190 | 225.85        | -2.05 | 1.31      | -3.36     | 0.180             | 19.4                  | 0.060             | 0.003             | -0.003            | 0.026             | 0.003             |
| 100 | 192 | 237.11        | -2.41 | 1.29      | -3.70     | 0.175             | 13.2                  | 0.060             | 0.005             | -0.002            | 0.028             | 0.000             |
| 102 | 138 | 87.37         | 2.43  | 1.70      | 0.72      | 0.500             | 19.9                  | 0.080             | -0.010            | 0.006             | 0.013             | 0.000             |
| 102 | 140 | 86.38         | 2.43  | 2.06      | 0.38      | 0.470             | 23.9                  | 0.080             | -0.006            | 0.006             | -0.002            | -0.003            |
| 102 | 142 | 85.94         | 2.40  | 2.13      | 0.26      | 0.470             | 23.9                  | 0.080             | -0.010            | 0.006             | -0.001            | 0.000             |
| 102 | 144 | 85.98         | 2.27  | 2.32      | -0.05     | 0.483             | 24.5                  | 0.080             | -0.012            | 0.008             | -0.001            | 0.002             |
| 102 | 146 | 86.61         | 2.16  | 2.39      | -0.22     | 0.492             | 24.0                  | 0.080             | -0.012            | 0.007             | 0.001             | 0.006             |

*Continued. . .*

Table 1 contd. . .

| Z   | N   | $M_{sp}^{th}$ | E     | $E_{mac}$ | $E_{mic}$ | $\beta_{20}^{sp}$ | $\gamma^{sp}(^{\circ})$ | $\beta_{40}^{sp}$ | $\beta_{42}^{sp}$ | $\beta_{44}^{sp}$ | $\beta_{60}^{sp}$ | $\beta_{80}^{sp}$ |
|-----|-----|---------------|-------|-----------|-----------|-------------------|-------------------------|-------------------|-------------------|-------------------|-------------------|-------------------|
| 102 | 148 | 87.80         | 2.07  | 2.35      | -0.28     | 0.498             | 22.5                    | 0.080             | -0.010            | 0.005             | 0.003             | 0.011             |
| 102 | 150 | 89.47         | 1.92  | 2.31      | -0.39     | 0.494             | 21.4                    | 0.080             | -0.004            | 0.005             | 0.002             | 0.012             |
| 102 | 152 | 91.46         | 1.57  | 2.11      | -0.55     | 0.487             | 19.2                    | 0.070             | 0.005             | 0.009             | 0.005             | 0.012             |
| 102 | 154 | 93.91         | 1.15  | 2.20      | -1.05     | 0.474             | 18.4                    | 0.080             | 0.009             | 0.004             | 0.002             | 0.011             |
| 102 | 156 | 96.64         | 0.51  | 2.35      | -1.84     | 0.424             | 19.3                    | 0.080             | 0.002             | -0.016            | -0.006            | 0.020             |
| 102 | 158 | 100.15        | 0.15  | 2.22      | -2.07     | 0.371             | 14.0                    | 0.080             | -0.003            | -0.022            | -0.013            | 0.023             |
| 102 | 160 | 104.28        | -0.06 | 2.61      | -2.67     | 0.388             | 11.9                    | 0.100             | 0.004             | -0.021            | -0.006            | 0.023             |
| 102 | 162 | 108.83        | -0.34 | 2.66      | -2.99     | 0.398             | 11.6                    | 0.100             | 0.003             | -0.022            | -0.008            | 0.024             |
| 102 | 164 | 113.91        | -0.55 | 2.52      | -3.07     | 0.410             | 12.7                    | 0.090             | 0.002             | -0.025            | -0.010            | 0.023             |
| 102 | 166 | 119.70        | -0.50 | 2.44      | -2.94     | 0.420             | 12.4                    | 0.090             | -0.003            | -0.024            | -0.014            | 0.019             |
| 102 | 168 | 125.92        | -0.48 | 2.20      | -2.68     | 0.420             | 12.4                    | 0.080             | -0.009            | -0.022            | -0.017            | 0.015             |
| 102 | 170 | 132.49        | -0.54 | 2.04      | -2.58     | 0.425             | 15.0                    | 0.060             | -0.010            | -0.026            | -0.014            | 0.008             |
| 102 | 172 | 139.34        | -0.75 | 1.03      | -1.79     | 0.300             | 0.0                     | 0.020             | 0.000             | 0.000             | 0.002             | 0.025             |
| 102 | 174 | 147.16        | -0.41 | 0.86      | -1.27     | 0.280             | 0.0                     | 0.010             | 0.000             | 0.000             | 0.008             | 0.017             |
| 102 | 176 | 155.21        | -0.26 | 0.86      | -1.12     | 0.280             | 0.0                     | 0.010             | 0.000             | 0.000             | 0.014             | 0.013             |
| 102 | 178 | 163.56        | -0.21 | 0.87      | -1.08     | 0.270             | 0.0                     | 0.020             | 0.000             | 0.000             | 0.019             | 0.010             |
| 102 | 180 | 172.20        | -0.28 | 0.91      | -1.18     | 0.270             | 2.1                     | 0.020             | -0.003            | 0.000             | 0.023             | 0.006             |
| 102 | 182 | 181.03        | -0.54 | 1.28      | -1.81     | 0.313             | 26.6                    | 0.020             | -0.006            | 0.002             | 0.014             | -0.003            |
| 102 | 184 | 190.14        | -0.90 | 1.28      | -2.18     | 0.304             | 27.4                    | 0.030             | -0.002            | 0.002             | 0.014             | -0.001            |
| 102 | 186 | 199.64        | -1.25 | 1.28      | -2.54     | 0.300             | 30.0                    | 0.030             | 0.002             | -0.001            | 0.010             | -0.004            |
| 102 | 188 | 209.47        | -1.64 | 1.20      | -2.84     | 0.261             | 32.5                    | 0.040             | 0.005             | -0.002            | 0.012             | -0.002            |
| 102 | 190 | 219.82        | -1.88 | 1.20      | -3.08     | 0.171             | 20.6                    | 0.060             | 0.002             | -0.003            | 0.023             | 0.004             |
| 102 | 192 | 230.49        | -2.15 | 1.17      | -3.32     | 0.153             | 11.3                    | 0.060             | 0.003             | -0.004            | 0.025             | 0.003             |
| 104 | 140 | 100.50        | 1.95  | 1.68      | 0.27      | 0.453             | 22.0                    | 0.090             | -0.009            | -0.016            | 0.002             | -0.001            |
| 104 | 142 | 99.18         | 1.88  | 2.07      | -0.18     | 0.457             | 23.2                    | 0.100             | -0.009            | -0.016            | 0.003             | 0.002             |
| 104 | 144 | 98.28         | 1.65  | 2.54      | -0.90     | 0.448             | 23.7                    | 0.110             | -0.011            | -0.022            | 0.002             | 0.006             |
| 104 | 146 | 97.96         | 1.43  | 2.45      | -1.02     | 0.439             | 24.2                    | 0.100             | -0.015            | -0.022            | -0.003            | 0.006             |
| 104 | 148 | 98.40         | 1.41  | 2.30      | -0.88     | 0.431             | 21.8                    | 0.100             | -0.012            | -0.021            | -0.001            | 0.008             |
| 104 | 150 | 99.28         | 1.29  | 1.99      | -0.70     | 0.427             | 20.6                    | 0.090             | -0.006            | -0.017            | -0.002            | 0.010             |
| 104 | 152 | 100.67        | 1.14  | 1.90      | -0.76     | 0.500             | 19.9                    | 0.090             | 0.004             | 0.007             | 0.002             | 0.009             |
| 104 | 154 | 102.28        | 0.69  | 1.51      | -0.82     | 0.392             | 19.4                    | 0.050             | -0.003            | -0.019            | -0.015            | 0.016             |
| 104 | 156 | 104.74        | 0.58  | 2.40      | -1.82     | 0.388             | 11.9                    | 0.110             | 0.003             | -0.021            | -0.002            | 0.018             |
| 104 | 158 | 107.31        | 0.08  | 2.42      | -2.34     | 0.398             | 11.6                    | 0.110             | 0.005             | -0.021            | -0.003            | 0.018             |
| 104 | 160 | 110.62        | -0.18 | 2.42      | -2.60     | 0.396             | 10.2                    | 0.110             | 0.005             | -0.019            | -0.007            | 0.020             |
| 104 | 162 | 114.16        | -0.69 | 2.28      | -2.98     | 0.408             | 11.3                    | 0.100             | 0.003             | -0.023            | -0.009            | 0.022             |
| 104 | 164 | 118.62        | -0.75 | 2.28      | -3.04     | 0.408             | 11.3                    | 0.100             | -0.002            | -0.022            | -0.012            | 0.022             |
| 104 | 166 | 123.47        | -0.89 | 2.08      | -2.98     | 0.430             | 12.1                    | 0.090             | -0.004            | -0.026            | -0.015            | 0.016             |
| 104 | 168 | 128.98        | -0.82 | 1.89      | -2.72     | 0.430             | 12.1                    | 0.080             | -0.009            | -0.025            | -0.017            | 0.013             |
| 104 | 170 | 134.80        | -0.88 | 1.98      | -2.86     | 0.432             | 13.4                    | 0.080             | -0.013            | -0.026            | -0.018            | 0.008             |
| 104 | 172 | 141.19        | -0.82 | 1.79      | -2.61     | 0.432             | 13.4                    | 0.070             | -0.015            | -0.024            | -0.017            | 0.006             |
| 104 | 174 | 148.13        | -0.62 | 0.86      | -1.48     | 0.290             | 0.0                     | 0.000             | 0.000             | 0.000             | 0.009             | 0.020             |
| 104 | 176 | 155.51        | -0.42 | 0.81      | -1.23     | 0.280             | 0.0                     | 0.000             | 0.000             | 0.000             | 0.015             | 0.015             |
| 104 | 178 | 163.19        | -0.32 | 0.78      | -1.09     | 0.270             | 0.0                     | 0.010             | 0.000             | 0.000             | 0.020             | 0.012             |
| 104 | 180 | 171.14        | -0.35 | 0.80      | -1.16     | 0.270             | 0.0                     | 0.010             | 0.000             | 0.000             | 0.024             | 0.008             |
| 104 | 182 | 179.41        | -0.47 | 0.80      | -1.27     | 0.260             | 0.0                     | 0.010             | 0.000             | 0.000             | 0.027             | 0.005             |
| 104 | 184 | 187.94        | -0.71 | 0.81      | -1.53     | 0.250             | 0.0                     | 0.020             | 0.000             | 0.000             | 0.028             | 0.003             |
| 104 | 186 | 196.82        | -0.98 | 1.26      | -2.24     | 0.314             | 30.7                    | 0.030             | -0.002            | 0.001             | 0.011             | -0.004            |
| 104 | 188 | 205.95        | -1.38 | 1.37      | -2.76     | 0.292             | 38.1                    | 0.040             | 0.003             | 0.000             | 0.005             | -0.003            |
| 104 | 190 | 215.51        | -1.73 | 0.91      | -2.63     | 0.166             | 25.0                    | 0.050             | 0.000             | -0.004            | 0.019             | 0.004             |
| 104 | 192 | 225.59        | -1.91 | 1.09      | -3.00     | 0.153             | 11.3                    | 0.060             | 0.003             | -0.003            | 0.022             | 0.004             |
| 106 | 142 | 113.98        | 1.25  | 1.80      | -0.55     | 0.448             | 23.7                    | 0.100             | -0.012            | -0.024            | 0.008             | 0.004             |
| 106 | 144 | 112.36        | 1.13  | 2.02      | -0.88     | 0.443             | 25.4                    | 0.100             | -0.015            | -0.022            | 0.005             | 0.004             |
| 106 | 146 | 111.34        | 1.04  | 1.72      | -0.67     | 0.429             | 27.8                    | 0.070             | -0.024            | -0.017            | -0.003            | 0.004             |
| 106 | 148 | 110.99        | 1.06  | 1.59      | -0.52     | 0.430             | 24.8                    | 0.070             | -0.025            | -0.018            | -0.002            | 0.008             |
| 106 | 150 | 111.19        | 1.07  | 1.37      | -0.30     | 0.416             | 24.1                    | 0.060             | -0.021            | -0.014            | -0.001            | 0.009             |
| 106 | 152 | 111.80        | 0.96  | 1.10      | -0.15     | 0.403             | 23.4                    | 0.040             | -0.011            | -0.010            | -0.005            | 0.012             |
| 106 | 154 | 112.96        | 0.85  | 2.39      | -1.54     | 0.398             | 11.6                    | 0.130             | 0.003             | -0.020            | 0.001             | 0.006             |
| 106 | 156 | 114.38        | 0.49  | 2.41      | -1.92     | 0.396             | 10.2                    | 0.130             | 0.005             | -0.018            | -0.002            | 0.008             |
| 106 | 158 | 116.25        | 0.07  | 2.15      | -2.07     | 0.404             | 8.5                     | 0.120             | 0.012             | -0.018            | -0.007            | 0.012             |
| 106 | 160 | 118.26        | -0.71 | 1.91      | -2.62     | 0.330             | 0.0                     | 0.080             | 0.000             | 0.000             | -0.023            | 0.040             |
| 106 | 162 | 121.44        | -0.81 | 1.85      | -2.65     | 0.330             | 0.0                     | 0.070             | 0.000             | 0.000             | -0.024            | 0.043             |
| 106 | 164 | 125.09        | -0.91 | 1.81      | -2.72     | 0.330             | 0.0                     | 0.060             | 0.000             | 0.000             | -0.024            | 0.046             |
| 106 | 166 | 129.18        | -1.05 | 1.68      | -2.73     | 0.330             | 0.0                     | 0.050             | 0.000             | 0.000             | -0.021            | 0.047             |
| 106 | 168 | 133.65        | -1.27 | 1.62      | -2.89     | 0.340             | 0.0                     | 0.050             | 0.000             | 0.000             | -0.017            | 0.046             |
| 106 | 170 | 138.92        | -1.13 | 1.59      | -2.72     | 0.439             | 11.8                    | 0.080             | -0.011            | -0.028            | -0.019            | 0.007             |
| 106 | 172 | 144.51        | -1.12 | 1.47      | -2.59     | 0.442             | 13.1                    | 0.070             | -0.009            | -0.027            | -0.019            | 0.006             |
| 106 | 174 | 150.85        | -0.80 | 0.92      | -1.73     | 0.300             | 0.0                     | -0.010            | 0.000             | 0.000             | 0.012             | 0.024             |

Continued. . .

Table 1 contd. . .

| Z   | N   | $M_{sp}^{th}$ | E     | $E_{mac}$ | $E_{mic}$ | $\beta_{20}^{sp}$ | $\gamma^{sp} (^{\circ})$ | $\beta_{40}^{sp}$ | $\beta_{42}^{sp}$ | $\beta_{44}^{sp}$ | $\beta_{60}^{sp}$ | $\beta_{80}^{sp}$ |
|-----|-----|---------------|-------|-----------|-----------|-------------------|--------------------------|-------------------|-------------------|-------------------|-------------------|-------------------|
| 106 | 176 | 157.50        | -0.59 | 0.87      | -1.46     | 0.290             | 0.0                      | -0.010            | 0.000             | 0.000             | 0.017             | 0.019             |
| 106 | 178 | 164.60        | -0.35 | 0.94      | -1.28     | 0.280             | 0.0                      | -0.020            | 0.000             | 0.000             | 0.022             | 0.013             |
| 106 | 180 | 171.88        | -0.35 | 0.84      | -1.19     | 0.270             | 0.0                      | -0.010            | 0.000             | 0.000             | 0.026             | 0.010             |
| 106 | 182 | 179.51        | -0.39 | 0.82      | -1.21     | 0.260             | 0.0                      | -0.010            | 0.000             | 0.000             | 0.027             | 0.007             |
| 106 | 184 | 187.39        | -0.58 | 0.68      | -1.27     | 0.240             | 0.0                      | 0.010             | 0.000             | 0.000             | 0.027             | 0.006             |
| 106 | 186 | 195.72        | -0.71 | 1.32      | -2.03     | 0.328             | 31.3                     | 0.040             | -0.007            | 0.002             | 0.013             | -0.005            |
| 106 | 188 | 204.16        | -1.11 | 1.21      | -2.32     | 0.323             | 29.8                     | 0.040             | -0.002            | 0.003             | 0.010             | -0.004            |
| 106 | 190 | 212.92        | -1.56 | 0.68      | -2.25     | 0.157             | 26.6                     | 0.040             | 0.000             | -0.004            | 0.018             | 0.006             |
| 106 | 192 | 222.41        | -1.65 | 0.81      | -2.46     | 0.143             | 12.1                     | 0.050             | 0.003             | -0.004            | 0.020             | 0.005             |
| 108 | 144 | 128.25        | 0.78  | 1.30      | -0.52     | 0.434             | 28.9                     | 0.070             | -0.025            | -0.016            | 0.000             | 0.006             |
| 108 | 146 | 126.37        | 0.65  | 1.28      | -0.62     | 0.429             | 27.8                     | 0.060             | -0.030            | -0.017            | -0.002            | 0.010             |
| 108 | 148 | 125.11        | 0.58  | 1.39      | -0.81     | 0.421             | 28.4                     | 0.050             | -0.034            | -0.017            | -0.005            | 0.012             |
| 108 | 150 | 124.66        | 0.75  | 1.04      | -0.30     | 0.420             | 25.4                     | 0.040             | -0.029            | -0.013            | 0.000             | 0.013             |
| 108 | 152 | 124.87        | 1.03  | 1.73      | -0.70     | 0.406             | 9.9                      | 0.130             | 0.010             | -0.014            | -0.001            | 0.001             |
| 108 | 154 | 124.76        | 0.47  | 1.84      | -1.38     | 0.416             | 9.7                      | 0.130             | 0.018             | -0.016            | -0.003            | -0.002            |
| 108 | 156 | 125.28        | -0.01 | 1.69      | -1.71     | 0.416             | 9.7                      | 0.120             | 0.019             | -0.019            | -0.006            | 0.004             |
| 108 | 158 | 126.26        | -0.54 | 1.78      | -2.31     | 0.340             | 0.0                      | 0.090             | 0.000             | 0.000             | -0.018            | 0.041             |
| 108 | 160 | 128.17        | -0.63 | 1.57      | -2.20     | 0.330             | 0.0                      | 0.070             | 0.001             | 0.000             | -0.018            | 0.045             |
| 108 | 162 | 130.59        | -0.72 | 1.59      | -2.30     | 0.330             | 0.0                      | 0.060             | 0.000             | 0.000             | -0.019            | 0.049             |
| 108 | 164 | 133.43        | -0.87 | 1.56      | -2.43     | 0.330             | 0.0                      | 0.050             | 0.000             | 0.000             | -0.017            | 0.051             |
| 108 | 166 | 136.62        | -1.15 | 1.53      | -2.68     | 0.340             | 0.0                      | 0.050             | 0.000             | 0.000             | -0.015            | 0.050             |
| 108 | 168 | 140.47        | -1.23 | 1.29      | -2.52     | 0.330             | 0.0                      | 0.040             | 0.000             | 0.000             | -0.007            | 0.047             |
| 108 | 170 | 144.69        | -1.41 | 1.07      | -2.49     | 0.330             | 0.0                      | 0.030             | 0.000             | 0.000             | 0.002             | 0.042             |
| 108 | 172 | 149.61        | -1.33 | 0.95      | -2.28     | 0.310             | 0.0                      | 0.000             | 0.000             | 0.000             | 0.012             | 0.034             |
| 108 | 174 | 155.36        | -0.87 | 1.03      | -1.90     | 0.300             | 0.0                      | -0.020            | 0.000             | 0.000             | 0.018             | 0.027             |
| 108 | 176 | 161.30        | -0.65 | 1.01      | -1.66     | 0.290             | 0.0                      | -0.020            | 0.000             | 0.000             | 0.024             | 0.022             |
| 108 | 178 | 167.63        | -0.46 | 1.01      | -1.47     | 0.280             | 0.0                      | -0.020            | 0.000             | 0.000             | 0.028             | 0.017             |
| 108 | 180 | 174.31        | -0.34 | 1.00      | -1.33     | 0.270             | 0.0                      | -0.020            | 0.000             | 0.000             | 0.031             | 0.013             |
| 108 | 182 | 181.08        | -0.54 | 2.01      | -2.55     | 0.400             | 36.9                     | 0.020             | -0.008            | -0.018            | 0.015             | -0.010            |
| 108 | 184 | 188.38        | -0.61 | 2.04      | -2.64     | 0.398             | 38.9                     | 0.020             | -0.005            | -0.017            | 0.009             | -0.011            |
| 108 | 186 | 195.95        | -0.79 | 2.04      | -2.83     | 0.398             | 38.9                     | 0.030             | -0.003            | -0.015            | 0.008             | -0.011            |
| 108 | 188 | 204.01        | -0.89 | 1.91      | -2.80     | 0.384             | 38.7                     | 0.040             | -0.002            | -0.012            | 0.006             | -0.010            |
| 108 | 190 | 212.06        | -1.37 | 0.73      | -2.11     | 0.288             | 20.3                     | 0.040             | -0.004            | 0.005             | 0.013             | -0.004            |
| 108 | 192 | 220.92        | -1.42 | 0.60      | -2.02     | 0.146             | 15.9                     | 0.040             | 0.004             | -0.005            | 0.018             | 0.005             |
| 110 | 146 | 142.96        | 0.18  | 1.01      | -0.83     | 0.434             | 28.9                     | 0.050             | -0.034            | -0.020            | 0.001             | 0.014             |
| 110 | 148 | 140.92        | 0.15  | 1.04      | -0.90     | 0.429             | 27.8                     | 0.040             | -0.038            | -0.020            | 0.002             | 0.015             |
| 110 | 150 | 139.72        | 0.38  | 0.81      | -0.43     | 0.430             | 24.8                     | 0.040             | -0.035            | -0.016            | 0.007             | 0.017             |
| 110 | 152 | 139.16        | 0.69  | 1.61      | -0.92     | 0.340             | 0.0                      | 0.120             | 0.000             | 0.000             | -0.010            | 0.020             |
| 110 | 154 | 138.41        | 0.27  | 1.39      | -1.12     | 0.350             | 0.0                      | 0.110             | 0.000             | 0.000             | -0.013            | 0.026             |
| 110 | 156 | 138.20        | -0.13 | 1.48      | -1.61     | 0.340             | 0.0                      | 0.100             | 0.000             | 0.000             | -0.014            | 0.034             |
| 110 | 158 | 138.58        | -0.47 | 1.18      | -1.65     | 0.330             | 0.0                      | 0.070             | 0.000             | 0.000             | -0.015            | 0.043             |
| 110 | 160 | 139.68        | -0.62 | 1.22      | -1.84     | 0.330             | 0.0                      | 0.070             | 0.001             | 0.000             | -0.013            | 0.043             |
| 110 | 162 | 141.30        | -0.73 | 1.28      | -2.01     | 0.330             | 0.0                      | 0.060             | 0.000             | 0.000             | -0.012            | 0.048             |
| 110 | 164 | 143.36        | -0.90 | 1.28      | -2.18     | 0.330             | 0.0                      | 0.040             | 0.000             | 0.000             | -0.010            | 0.053             |
| 110 | 166 | 145.81        | -1.17 | 1.19      | -2.36     | 0.340             | 0.0                      | 0.040             | 0.000             | 0.000             | -0.008            | 0.051             |
| 110 | 168 | 148.86        | -1.30 | 1.05      | -2.36     | 0.330             | 0.0                      | 0.030             | 0.000             | 0.000             | 0.001             | 0.047             |
| 110 | 170 | 152.36        | -1.45 | 0.97      | -2.42     | 0.320             | 0.0                      | 0.010             | 0.000             | 0.000             | 0.012             | 0.042             |
| 110 | 172 | 156.74        | -1.18 | 1.10      | -2.28     | 0.300             | 0.0                      | -0.020            | 0.000             | 0.000             | 0.021             | 0.034             |
| 110 | 174 | 161.68        | -0.79 | 1.26      | -2.05     | 0.290             | 0.0                      | -0.030            | 0.000             | 0.000             | 0.029             | 0.027             |
| 110 | 176 | 166.92        | -0.55 | 1.30      | -1.85     | 0.280             | 0.0                      | -0.030            | 0.000             | 0.000             | 0.035             | 0.023             |
| 110 | 178 | 172.49        | -0.41 | 1.33      | -1.73     | 0.280             | 0.0                      | -0.030            | 0.000             | 0.000             | 0.038             | 0.019             |
| 110 | 180 | 178.31        | -0.43 | 1.87      | -2.30     | 0.414             | 37.2                     | 0.030             | -0.006            | -0.015            | 0.019             | -0.006            |
| 110 | 182 | 184.26        | -0.74 | 1.89      | -2.63     | 0.414             | 37.2                     | 0.030             | -0.006            | -0.017            | 0.017             | -0.008            |
| 110 | 184 | 190.85        | -0.82 | 1.84      | -2.66     | 0.405             | 40.0                     | 0.030             | -0.003            | -0.009            | 0.011             | -0.009            |
| 110 | 186 | 197.69        | -1.05 | 1.98      | -3.03     | 0.419             | 40.2                     | 0.030             | 0.000             | -0.010            | 0.008             | -0.010            |
| 110 | 188 | 205.04        | -1.17 | 1.17      | -2.34     | 0.402             | 26.6                     | 0.020             | -0.029            | -0.008            | 0.011             | -0.011            |
| 110 | 190 | 212.81        | -1.24 | 0.58      | -1.82     | 0.275             | 19.1                     | 0.040             | -0.003            | 0.006             | 0.014             | -0.001            |
| 110 | 192 | 221.00        | -1.27 | 0.43      | -1.70     | 0.148             | 28.3                     | 0.030             | 0.000             | -0.006            | 0.015             | 0.004             |
| 112 | 148 | 158.71        | 0.08  | 0.66      | -0.58     | 0.434             | 26.0                     | 0.030             | -0.040            | -0.023            | 0.013             | 0.019             |
| 112 | 150 | 157.02        | 0.63  | 0.12      | 0.52      | 0.431             | 21.8                     | 0.030             | -0.024            | -0.013            | 0.014             | 0.023             |
| 112 | 152 | 155.34        | 0.63  | 0.69      | -0.06     | 0.340             | 0.0                      | 0.100             | 0.000             | 0.000             | -0.010            | 0.020             |
| 112 | 154 | 153.79        | 0.20  | 0.70      | -0.50     | 0.340             | 0.0                      | 0.090             | 0.000             | 0.000             | -0.012            | 0.029             |
| 112 | 156 | 152.75        | -0.26 | 0.72      | -0.98     | 0.340             | 0.0                      | 0.080             | 0.000             | 0.000             | -0.012            | 0.036             |
| 112 | 158 | 152.43        | -0.52 | 0.67      | -1.18     | 0.330             | 0.0                      | 0.060             | 0.000             | 0.000             | -0.010            | 0.041             |
| 112 | 160 | 152.82        | -0.60 | 0.76      | -1.35     | 0.330             | 0.0                      | 0.040             | 0.000             | 0.000             | -0.009            | 0.048             |
| 112 | 162 | 153.62        | -0.77 | 0.88      | -1.65     | 0.330             | 0.0                      | 0.040             | 0.000             | 0.000             | -0.007            | 0.050             |
| 112 | 164 | 154.93        | -0.92 | 0.93      | -1.86     | 0.330             | 0.0                      | 0.030             | 0.000             | 0.000             | -0.003            | 0.052             |

Continued. . .

Table 1 contd. . .

| Z   | N   | $M_{sp}^{th}$ | E     | $E_{mac}$ | $E_{mic}$ | $\beta_{20}^{sp}$ | $\gamma^{sp} (^{\circ})$ | $\beta_{40}^{sp}$ | $\beta_{42}^{sp}$ | $\beta_{44}^{sp}$ | $\beta_{60}^{sp}$ | $\beta_{80}^{sp}$ |
|-----|-----|---------------|-------|-----------|-----------|-------------------|--------------------------|-------------------|-------------------|-------------------|-------------------|-------------------|
| 112 | 166 | 156.75        | -1.07 | 0.85      | -1.92     | 0.330             | 0.0                      | 0.020             | 0.000             | 0.000             | 0.003             | 0.049             |
| 112 | 168 | 158.91        | -1.35 | 0.82      | -2.16     | 0.330             | 0.0                      | 0.020             | 0.000             | 0.000             | 0.009             | 0.046             |
| 112 | 170 | 162.01        | -1.15 | 1.08      | -2.23     | 0.300             | 0.0                      | -0.020            | 0.000             | 0.000             | 0.024             | 0.037             |
| 112 | 172 | 165.72        | -0.82 | 1.28      | -2.10     | 0.290             | 0.0                      | -0.030            | 0.000             | 0.000             | 0.033             | 0.031             |
| 112 | 174 | 169.89        | -0.48 | 1.66      | -2.13     | 0.280             | 0.0                      | -0.040            | 0.000             | 0.000             | 0.043             | 0.025             |
| 112 | 176 | 174.27        | -0.36 | 1.70      | -2.06     | 0.419             | 33.3                     | 0.020             | -0.023            | -0.026            | 0.024             | -0.005            |
| 112 | 178 | 178.92        | -0.42 | 1.50      | -1.92     | 0.424             | 34.5                     | 0.030             | -0.013            | -0.016            | 0.022             | -0.004            |
| 112 | 180 | 183.77        | -0.71 | 1.53      | -2.24     | 0.424             | 34.5                     | 0.030             | -0.012            | -0.017            | 0.021             | -0.007            |
| 112 | 182 | 189.08        | -0.96 | 1.60      | -2.56     | 0.430             | 35.6                     | 0.030             | -0.010            | -0.017            | 0.018             | -0.009            |
| 112 | 184 | 194.67        | -1.33 | 1.33      | -2.66     | 0.341             | 58.2                     | 0.010             | -0.002            | 0.000             | -0.003            | -0.003            |
| 112 | 186 | 201.15        | -1.24 | 1.13      | -2.36     | 0.316             | 55.3                     | 0.020             | -0.012            | 0.007             | -0.002            | -0.003            |
| 112 | 188 | 208.12        | -1.04 | 0.90      | -1.93     | 0.286             | 53.6                     | 0.020             | -0.011            | 0.007             | -0.001            | -0.002            |
| 112 | 190 | 215.14        | -1.19 | 0.47      | -1.65     | 0.288             | 20.3                     | 0.040             | -0.005            | 0.010             | 0.013             | -0.001            |
| 112 | 192 | 222.61        | -1.26 | 0.21      | -1.47     | 0.158             | 55.3                     | 0.000             | -0.003            | 0.002             | 0.000             | -0.001            |
| 114 | 150 | 175.66        | 0.63  | -0.35     | 0.98      | 0.350             | 0.0                      | 0.080             | 0.000             | 0.000             | -0.007            | 0.015             |
| 114 | 152 | 172.88        | 0.32  | -0.18     | 0.50      | 0.350             | 0.0                      | 0.080             | 0.000             | 0.000             | -0.008            | 0.022             |
| 114 | 154 | 170.53        | -0.12 | -0.02     | -0.10     | 0.340             | 0.0                      | 0.070             | 0.000             | 0.000             | -0.010            | 0.029             |
| 114 | 156 | 168.82        | -0.46 | 0.11      | -0.57     | 0.330             | 0.0                      | 0.060             | 0.000             | 0.000             | -0.009            | 0.034             |
| 114 | 158 | 167.96        | -0.49 | 0.22      | -0.71     | 0.320             | 0.0                      | 0.040             | 0.000             | 0.000             | -0.007            | 0.040             |
| 114 | 160 | 167.61        | -0.53 | 0.42      | -0.95     | 0.320             | 0.0                      | 0.030             | 0.000             | 0.000             | -0.004            | 0.046             |
| 114 | 162 | 167.71        | -0.64 | 0.55      | -1.19     | 0.330             | 0.0                      | 0.020             | 0.000             | 0.000             | -0.001            | 0.050             |
| 114 | 164 | 168.29        | -0.77 | 0.64      | -1.40     | 0.320             | 0.0                      | 0.020             | 0.000             | 0.000             | 0.005             | 0.049             |
| 114 | 166 | 169.34        | -0.93 | 0.68      | -1.61     | 0.320             | 0.0                      | 0.010             | 0.000             | 0.000             | 0.013             | 0.047             |
| 114 | 168 | 170.99        | -0.97 | 0.91      | -1.88     | 0.310             | 0.0                      | -0.010            | 0.000             | 0.000             | 0.024             | 0.042             |
| 114 | 170 | 173.46        | -0.68 | 1.28      | -1.96     | 0.290             | 0.0                      | -0.030            | 0.000             | 0.000             | 0.036             | 0.034             |
| 114 | 172 | 176.37        | -0.41 | 1.70      | -2.10     | 0.290             | 0.0                      | -0.040            | 0.000             | 0.000             | 0.046             | 0.029             |
| 114 | 174 | 179.71        | -0.17 | 1.66      | -1.83     | 0.270             | 0.0                      | -0.030            | 0.000             | 0.000             | 0.051             | 0.025             |
| 114 | 176 | 183.20        | -0.22 | 1.13      | -1.35     | 0.433             | 33.7                     | 0.030             | -0.019            | -0.015            | 0.023             | -0.003            |
| 114 | 178 | 186.94        | -0.48 | 1.12      | -1.59     | 0.433             | 33.7                     | 0.030             | -0.016            | -0.014            | 0.022             | -0.006            |
| 114 | 180 | 191.18        | -0.67 | 1.19      | -1.85     | 0.438             | 34.8                     | 0.030             | -0.012            | -0.013            | 0.020             | -0.008            |
| 114 | 182 | 195.27        | -1.43 | 1.34      | -2.77     | 0.444             | 31.2                     | 0.020             | -0.030            | -0.026            | 0.016             | -0.013            |
| 114 | 184 | 199.98        | -1.99 | 1.54      | -3.53     | 0.457             | 28.8                     | 0.010             | -0.040            | -0.031            | 0.012             | -0.016            |
| 114 | 186 | 206.11        | -1.54 | 0.98      | -2.53     | 0.311             | 56.9                     | 0.020             | -0.016            | 0.013             | -0.002            | -0.003            |
| 114 | 188 | 212.45        | -1.29 | 0.98      | -2.26     | 0.300             | 53.2                     | 0.030             | -0.018            | 0.011             | 0.000             | -0.002            |
| 114 | 190 | 218.91        | -1.31 | 1.05      | -2.36     | 0.286             | 36.5                     | 0.060             | -0.010            | 0.015             | 0.009             | 0.000             |
| 114 | 192 | 225.57        | -1.53 | 0.15      | -1.68     | 0.294             | 17.8                     | 0.030             | -0.006            | 0.007             | 0.011             | -0.005            |
| 116 | 152 | 191.89        | -0.09 | -0.69     | 0.60      | 0.330             | 0.0                      | 0.050             | 0.000             | 0.000             | -0.008            | 0.023             |
| 116 | 154 | 188.92        | -0.36 | -0.44     | 0.08      | 0.320             | 0.0                      | 0.050             | 0.001             | 0.001             | -0.009            | 0.027             |
| 116 | 156 | 186.82        | -0.32 | -0.32     | 0.00      | 0.310             | 0.0                      | 0.030             | 0.000             | 0.000             | -0.006            | 0.032             |
| 116 | 158 | 185.30        | -0.23 | -0.10     | -0.13     | 0.310             | 0.0                      | 0.020             | 0.000             | 0.000             | -0.003            | 0.039             |
| 116 | 160 | 184.22        | -0.24 | 0.10      | -0.34     | 0.310             | 0.0                      | 0.020             | 0.000             | 0.000             | 0.001             | 0.043             |
| 116 | 162 | 183.53        | -0.37 | 0.25      | -0.63     | 0.320             | 0.0                      | 0.010             | 0.000             | 0.000             | 0.006             | 0.046             |
| 116 | 164 | 183.45        | -0.41 | 0.38      | -0.79     | 0.310             | 0.0                      | 0.010             | 0.000             | 0.000             | 0.014             | 0.044             |
| 116 | 166 | 183.71        | -0.60 | 0.55      | -1.16     | 0.310             | 0.0                      | 0.000             | 0.000             | 0.000             | 0.022             | 0.043             |
| 116 | 168 | 184.69        | -0.58 | 0.97      | -1.54     | 0.300             | 0.0                      | -0.020            | 0.000             | 0.000             | 0.034             | 0.038             |
| 116 | 170 | 186.37        | -0.34 | 1.33      | -1.67     | 0.290             | 0.0                      | -0.030            | 0.000             | 0.000             | 0.044             | 0.033             |
| 116 | 172 | 188.49        | -0.12 | 1.96      | -2.08     | 0.280             | 0.0                      | -0.040            | 0.000             | 0.000             | 0.056             | 0.028             |
| 116 | 174 | 191.14        | 0.16  | 0.73      | -0.58     | 0.444             | 35.9                     | 0.030             | -0.013            | 0.006             | 0.024             | -0.003            |
| 116 | 176 | 193.74        | -0.07 | 0.68      | -0.76     | 0.438             | 34.8                     | 0.040             | -0.011            | 0.000             | 0.022             | -0.002            |
| 116 | 178 | 196.71        | -0.39 | 0.70      | -1.09     | 0.438             | 34.8                     | 0.030             | -0.012            | -0.003            | 0.022             | -0.006            |
| 116 | 180 | 200.04        | -0.77 | 0.65      | -1.43     | 0.441             | 33.0                     | 0.030             | -0.018            | -0.011            | 0.018             | -0.010            |
| 116 | 182 | 203.46        | -1.51 | 0.99      | -2.50     | 0.453             | 30.5                     | 0.020             | -0.033            | -0.027            | 0.014             | -0.016            |
| 116 | 184 | 207.88        | -1.66 | 1.09      | -2.75     | 0.453             | 30.5                     | 0.010             | -0.034            | -0.026            | 0.014             | -0.019            |
| 116 | 186 | 212.65        | -1.88 | 1.25      | -3.13     | 0.457             | 28.8                     | 0.000             | -0.040            | -0.029            | 0.010             | -0.019            |
| 116 | 188 | 218.34        | -1.59 | 0.87      | -2.46     | 0.448             | 29.4                     | 0.010             | -0.034            | -0.022            | 0.008             | -0.018            |
| 116 | 190 | 224.42        | -1.32 | 0.46      | -1.78     | 0.286             | 24.8                     | 0.050             | -0.003            | 0.017             | 0.013             | 0.002             |
| 116 | 192 | 230.30        | -1.64 | 0.00      | -1.63     | 0.301             | 15.4                     | 0.040             | -0.010            | 0.006             | 0.013             | -0.006            |
| 118 | 154 | 209.46        | -0.01 | -0.75     | 0.74      | 0.300             | 0.0                      | 0.030             | 0.000             | 0.000             | -0.008            | 0.023             |
| 118 | 156 | 206.74        | 0.19  | -0.53     | 0.72      | 0.290             | 0.0                      | 0.030             | 0.000             | 0.000             | -0.004            | 0.028             |
| 118 | 158 | 204.35        | 0.18  | -0.40     | 0.58      | 0.300             | 0.0                      | 0.020             | 0.000             | 0.000             | 0.002             | 0.034             |
| 118 | 160 | 202.34        | 0.01  | -0.26     | 0.26      | 0.310             | 0.0                      | 0.020             | 0.000             | 0.000             | 0.007             | 0.039             |
| 118 | 162 | 200.93        | -0.09 | -0.10     | 0.01      | 0.310             | 0.0                      | 0.020             | 0.000             | 0.000             | 0.012             | 0.041             |
| 118 | 164 | 200.07        | -0.15 | 0.21      | -0.35     | 0.310             | 0.0                      | 0.000             | 0.000             | 0.000             | 0.022             | 0.041             |
| 118 | 166 | 199.60        | -0.34 | 0.50      | -0.83     | 0.310             | 0.0                      | -0.010            | 0.000             | 0.000             | 0.030             | 0.040             |
| 118 | 168 | 199.82        | -0.32 | 0.85      | -1.17     | 0.300             | 0.0                      | -0.020            | 0.000             | 0.000             | 0.039             | 0.036             |
| 118 | 170 | 200.85        | 0.00  | 0.58      | -0.57     | 0.464             | 37.1                     | 0.010             | -0.021            | 0.021             | 0.025             | -0.009            |
| 118 | 172 | 201.99        | -0.03 | 0.60      | -0.63     | 0.464             | 37.1                     | 0.010             | -0.017            | 0.021             | 0.024             | -0.008            |

Continued. . .

Table 1 contd. . .

| Z   | N   | $M_{sp}^{th}$ | E     | $E_{mac}$ | $E_{mic}$ | $\beta_{20}^{sp}$ | $\gamma^{sp}(^{\circ})$ | $\beta_{40}^{sp}$ | $\beta_{42}^{sp}$ | $\beta_{44}^{sp}$ | $\beta_{60}^{sp}$ | $\beta_{80}^{sp}$ |
|-----|-----|---------------|-------|-----------|-----------|-------------------|-------------------------|-------------------|-------------------|-------------------|-------------------|-------------------|
| 118 | 174 | 203.62        | -0.05 | 0.49      | -0.54     | 0.450             | 36.9                    | 0.020             | -0.017            | 0.014             | 0.025             | -0.007            |
| 118 | 176 | 205.62        | -0.17 | 0.38      | -0.55     | 0.444             | 35.9                    | 0.030             | -0.013            | 0.007             | 0.024             | -0.006            |
| 118 | 178 | 207.91        | -0.45 | 0.39      | -0.84     | 0.444             | 35.9                    | 0.030             | -0.011            | 0.004             | 0.022             | -0.008            |
| 118 | 180 | 210.64        | -0.73 | 0.24      | -0.97     | 0.447             | 34.1                    | 0.030             | -0.012            | -0.001            | 0.018             | -0.011            |
| 118 | 182 | 213.46        | -1.36 | 0.44      | -1.80     | 0.453             | 30.5                    | 0.020             | -0.028            | -0.023            | 0.015             | -0.018            |
| 118 | 184 | 217.23        | -1.47 | 0.45      | -1.92     | 0.453             | 30.5                    | 0.020             | -0.026            | -0.022            | 0.014             | -0.020            |
| 118 | 186 | 221.32        | -1.68 | 0.55      | -2.23     | 0.461             | 29.9                    | 0.010             | -0.031            | -0.024            | 0.011             | -0.020            |
| 118 | 188 | 226.19        | -1.53 | 0.39      | -1.92     | 0.453             | 30.5                    | 0.010             | -0.025            | -0.018            | 0.007             | -0.019            |
| 118 | 190 | 231.40        | -1.44 | 0.35      | -1.78     | 0.453             | 30.5                    | 0.010             | -0.025            | -0.016            | 0.004             | -0.017            |
| 118 | 192 | 236.67        | -1.70 | -0.15     | -1.55     | 0.304             | 17.3                    | 0.040             | -0.008            | 0.009             | 0.013             | -0.006            |
| 120 | 156 | 226.20        | -1.30 | -0.27     | -1.02     | 0.490             | 39.2                    | 0.040             | -0.047            | -0.001            | 0.019             | 0.002             |
| 120 | 158 | 223.09        | -1.26 | -0.20     | -1.06     | 0.492             | 37.6                    | 0.050             | -0.051            | -0.001            | 0.022             | 0.003             |
| 120 | 160 | 220.58        | -1.17 | 0.05      | -1.22     | 0.498             | 38.5                    | 0.040             | -0.053            | -0.002            | 0.025             | -0.001            |
| 120 | 162 | 218.76        | -0.92 | 0.18      | -1.10     | 0.498             | 38.5                    | 0.030             | -0.053            | 0.001             | 0.026             | -0.003            |
| 120 | 164 | 217.57        | -0.57 | 0.23      | -0.80     | 0.490             | 39.2                    | 0.030             | -0.047            | 0.009             | 0.027             | -0.005            |
| 120 | 166 | 216.76        | -0.35 | 0.33      | -0.68     | 0.483             | 40.0                    | 0.020             | -0.041            | 0.016             | 0.027             | -0.008            |
| 120 | 168 | 216.40        | -0.18 | 0.33      | -0.51     | 0.469             | 39.8                    | 0.010             | -0.028            | 0.023             | 0.026             | -0.009            |
| 120 | 170 | 216.44        | -0.10 | 0.30      | -0.40     | 0.455             | 39.7                    | 0.010             | -0.023            | 0.023             | 0.024             | -0.009            |
| 120 | 172 | 216.91        | -0.08 | 0.16      | -0.25     | 0.456             | 37.9                    | 0.020             | -0.017            | 0.020             | 0.027             | -0.006            |
| 120 | 174 | 217.83        | -0.09 | 0.08      | -0.18     | 0.450             | 36.9                    | 0.030             | -0.013            | 0.015             | 0.027             | -0.006            |
| 120 | 176 | 219.07        | -0.25 | -0.02     | -0.23     | 0.444             | 35.9                    | 0.030             | -0.008            | 0.009             | 0.025             | -0.007            |
| 120 | 178 | 220.69        | -0.49 | -0.01     | -0.48     | 0.444             | 35.9                    | 0.020             | -0.008            | 0.006             | 0.021             | -0.010            |
| 120 | 180 | 222.68        | -0.81 | 0.00      | -0.81     | 0.444             | 35.9                    | 0.030             | -0.006            | 0.002             | 0.019             | -0.011            |
| 120 | 182 | 225.12        | -1.12 | -0.28     | -0.83     | 0.449             | 32.3                    | 0.020             | -0.008            | -0.004            | 0.011             | -0.015            |
| 120 | 184 | 228.07        | -1.35 | -0.17     | -1.19     | 0.449             | 32.3                    | 0.020             | -0.010            | -0.007            | 0.012             | -0.018            |
| 120 | 186 | 231.42        | -1.61 | -0.08     | -1.53     | 0.461             | 29.9                    | 0.010             | -0.021            | -0.020            | 0.008             | -0.021            |
| 120 | 188 | 235.58        | -1.49 | -0.16     | -1.32     | 0.453             | 30.5                    | 0.010             | -0.013            | -0.014            | 0.004             | -0.019            |
| 120 | 190 | 240.11        | -1.41 | -0.20     | -1.22     | 0.453             | 30.5                    | 0.010             | -0.011            | -0.013            | -0.001            | -0.016            |
| 120 | 192 | 245.01        | -1.36 | -0.28     | -1.08     | 0.461             | 29.9                    | 0.010             | -0.011            | -0.012            | -0.003            | -0.014            |
| 122 | 158 | 244.85        | -1.21 | -0.57     | -0.64     | 0.497             | 40.1                    | 0.050             | -0.051            | -0.002            | 0.019             | 0.005             |
| 122 | 160 | 241.32        | -1.37 | -0.46     | -0.91     | 0.498             | 38.5                    | 0.040             | -0.059            | -0.001            | 0.023             | 0.003             |
| 122 | 162 | 238.77        | -1.10 | -0.30     | -0.80     | 0.504             | 39.4                    | 0.040             | -0.057            | 0.002             | 0.025             | 0.003             |
| 122 | 164 | 236.77        | -0.81 | -0.22     | -0.59     | 0.504             | 39.4                    | 0.040             | -0.054            | 0.008             | 0.028             | 0.003             |
| 122 | 166 | 235.24        | -0.57 | -0.06     | -0.51     | 0.497             | 40.1                    | 0.030             | -0.054            | 0.015             | 0.026             | 0.001             |
| 122 | 168 | 234.43        | -0.12 | -0.06     | -0.06     | 0.468             | 41.6                    | 0.020             | -0.035            | 0.021             | 0.025             | -0.006            |
| 122 | 170 | 233.81        | 0.04  | -0.17     | 0.21      | 0.461             | 40.6                    | 0.020             | -0.021            | 0.022             | 0.025             | -0.006            |
| 122 | 172 | 233.62        | 0.11  | -0.33     | 0.44      | 0.448             | 38.7                    | 0.020             | -0.009            | 0.018             | 0.023             | -0.004            |
| 122 | 174 | 233.77        | 0.06  | -0.35     | 0.40      | 0.442             | 37.7                    | 0.010             | -0.001            | 0.013             | 0.018             | -0.005            |
| 122 | 176 | 234.22        | -0.18 | -0.39     | 0.21      | 0.436             | 36.6                    | 0.020             | 0.002             | 0.007             | 0.019             | -0.006            |
| 122 | 178 | 235.09        | -0.45 | -0.32     | -0.13     | 0.436             | 36.6                    | 0.020             | 0.003             | 0.003             | 0.018             | -0.008            |
| 122 | 180 | 236.33        | -0.82 | -0.28     | -0.55     | 0.436             | 36.6                    | 0.030             | 0.004             | -0.001            | 0.016             | -0.010            |
| 122 | 182 | 238.01        | -1.19 | -0.22     | -0.97     | 0.436             | 36.6                    | 0.030             | 0.004             | -0.004            | 0.014             | -0.013            |
| 122 | 184 | 240.18        | -1.51 | -0.71     | -0.81     | 0.458             | 31.6                    | 0.020             | -0.001            | -0.004            | 0.007             | -0.018            |
| 122 | 186 | 242.95        | -1.67 | -0.70     | -0.98     | 0.461             | 29.9                    | 0.010             | -0.009            | -0.013            | 0.004             | -0.020            |
| 122 | 188 | 246.37        | -1.61 | -0.62     | -0.99     | 0.453             | 30.5                    | 0.010             | -0.002            | -0.010            | 0.000             | -0.018            |
| 122 | 190 | 249.94        | -1.81 | -0.16     | -1.64     | 0.305             | 23.2                    | 0.050             | -0.001            | 0.021             | 0.015             | -0.003            |
| 122 | 192 | 253.87        | -2.07 | -0.34     | -1.72     | 0.310             | 20.8                    | 0.050             | 0.002             | 0.017             | 0.010             | -0.007            |
| 124 | 160 | 263.66        | -1.48 | -1.01     | -0.48     | 0.498             | 38.5                    | 0.040             | -0.064            | -0.001            | 0.021             | 0.005             |
| 124 | 162 | 260.38        | -1.19 | -0.81     | -0.39     | 0.504             | 39.4                    | 0.050             | -0.061            | 0.002             | 0.026             | 0.006             |
| 124 | 164 | 257.52        | -1.01 | -0.68     | -0.33     | 0.511             | 40.3                    | 0.050             | -0.057            | 0.010             | 0.029             | 0.007             |
| 124 | 166 | 255.20        | -0.82 | -0.52     | -0.31     | 0.503             | 41.0                    | 0.040             | -0.057            | 0.015             | 0.026             | 0.004             |
| 124 | 168 | 253.79        | -0.23 | -0.45     | 0.22      | 0.482             | 41.7                    | 0.030             | -0.050            | 0.019             | 0.023             | 0.000             |
| 124 | 170 | 252.72        | 0.19  | -0.74     | 0.93      | 0.461             | 40.6                    | 0.020             | -0.012            | 0.022             | 0.022             | -0.004            |
| 124 | 172 | 251.77        | 0.23  | -0.71     | 0.94      | 0.440             | 39.5                    | 0.020             | 0.004             | 0.015             | 0.017             | -0.001            |
| 124 | 174 | 251.10        | 0.07  | -0.68     | 0.76      | 0.434             | 38.5                    | 0.020             | 0.009             | 0.009             | 0.016             | -0.003            |
| 124 | 176 | 250.77        | -0.23 | -0.65     | 0.42      | 0.428             | 37.4                    | 0.030             | 0.012             | 0.003             | 0.016             | -0.004            |
| 124 | 178 | 250.88        | -0.56 | -0.56     | 0.00      | 0.428             | 37.4                    | 0.030             | 0.015             | 0.000             | 0.012             | -0.005            |
| 124 | 180 | 251.42        | -0.92 | -0.47     | -0.46     | 0.428             | 37.4                    | 0.030             | 0.014             | -0.004            | 0.014             | -0.009            |
| 124 | 182 | 252.41        | -1.29 | -0.39     | -0.91     | 0.428             | 37.4                    | 0.040             | 0.013             | -0.006            | 0.013             | -0.011            |
| 124 | 184 | 253.84        | -1.67 | -0.46     | -1.21     | 0.436             | 36.6                    | 0.030             | 0.010             | -0.008            | 0.010             | -0.015            |
| 124 | 186 | 255.88        | -1.87 | -1.18     | -0.69     | 0.461             | 29.9                    | 0.010             | -0.001            | -0.008            | 0.001             | -0.020            |
| 124 | 188 | 258.64        | -1.78 | 0.18      | -1.96     | 0.304             | 27.4                    | 0.070             | 0.001             | 0.026             | 0.016             | 0.001             |
| 124 | 190 | 261.43        | -2.08 | -0.37     | -1.71     | 0.305             | 23.2                    | 0.050             | 0.002             | 0.021             | 0.015             | -0.005            |
| 124 | 192 | 264.66        | -2.37 | -0.41     | -1.96     | 0.305             | 23.2                    | 0.050             | 0.002             | 0.020             | 0.010             | -0.006            |
| 126 | 162 | 283.37        | -1.38 | -1.48     | 0.10      | 0.511             | 40.3                    | 0.060             | -0.059            | 0.004             | 0.025             | 0.007             |
| 126 | 164 | 279.69        | -1.28 | -1.35     | 0.07      | 0.511             | 40.3                    | 0.050             | -0.060            | 0.009             | 0.027             | 0.006             |
| 126 | 166 | 276.70        | -1.03 | -1.09     | 0.07      | 0.503             | 41.0                    | 0.050             | -0.057            | 0.016             | 0.029             | 0.005             |

Continued. . .

Table 1 contd. . .

| Z    | N   | $M_{sp}^{th}$ | E     | $E_{mac}$ | $E_{mic}$ | $\beta_{20}^{sp}$ | $\gamma^{sp}(^{\circ})$ | $\beta_{40}^{sp}$ | $\beta_{42}^{sp}$ | $\beta_{44}^{sp}$ | $\beta_{60}^{sp}$ | $\beta_{80}^{sp}$ |
|------|-----|---------------|-------|-----------|-----------|-------------------|-------------------------|-------------------|-------------------|-------------------|-------------------|-------------------|
| 126  | 168 | 274.31        | -0.69 | -0.85     | 0.17      | 0.496             | 41.8                    | 0.050             | -0.056            | 0.019             | 0.028             | 0.005             |
| 126  | 170 | 272.82        | 0.05  | -0.91     | 0.96      | 0.482             | 41.7                    | 0.030             | -0.050            | 0.022             | 0.025             | 0.002             |
| 126  | 172 | 271.22        | 0.16  | -0.98     | 1.14      | 0.453             | 41.4                    | 0.020             | 0.011             | 0.017             | 0.012             | 0.000             |
| 126  | 174 | 269.79        | -0.05 | -0.93     | 0.89      | 0.426             | 39.3                    | 0.030             | 0.016             | 0.006             | 0.012             | -0.001            |
| 126  | 176 | 268.64        | -0.46 | -1.03     | 0.56      | 0.422             | 36.3                    | 0.030             | 0.018             | 0.001             | 0.014             | -0.005            |
| 126  | 178 | 268.05        | -0.79 | -0.84     | 0.05      | 0.428             | 37.4                    | 0.030             | 0.020             | -0.003            | 0.012             | -0.007            |
| 126  | 180 | 267.88        | -1.16 | -0.73     | -0.43     | 0.428             | 37.4                    | 0.030             | 0.020             | -0.007            | 0.012             | -0.010            |
| 126  | 182 | 268.19        | -1.52 | -0.63     | -0.89     | 0.428             | 37.4                    | 0.030             | 0.021             | -0.009            | 0.009             | -0.011            |
| 126  | 184 | 269.02        | -1.80 | -0.46     | -1.33     | 0.426             | 39.3                    | 0.040             | 0.018             | -0.008            | 0.009             | -0.012            |
| 126  | 186 | 270.62        | -1.76 | -0.03     | -1.73     | 0.304             | 27.4                    | 0.070             | 0.002             | 0.028             | 0.019             | 0.001             |
| 126  | 188 | 272.22        | -2.15 | -0.37     | -1.78     | 0.309             | 24.9                    | 0.060             | 0.004             | 0.025             | 0.015             | -0.003            |
| 126  | 190 | 274.31        | -2.49 | -0.70     | -1.79     | 0.314             | 22.5                    | 0.050             | 0.003             | 0.022             | 0.012             | -0.009            |
| *126 | 192 | 276.92        | -2.72 | -0.46     | -2.26     | 0.305             | 23.2                    | 0.060             | 0.005             | 0.022             | 0.008             | -0.008            |

\* marginally unbound nucleus

## References

- [1] Yu. Ts. Oganessian et al., *Phys. Rev. Lett.* **83**, 3154 (1999).
- [2] Yu. Ts. Oganessian et al., *Nature* (London) **400**, 242 (1999).
- [3] Yu. Ts. Oganessian et al., *Phys. Rev. C*, **62**, 041604 (2000).
- [4] Yu. Ts. Oganessian et al., *Phys. Rev. C*, **63**, 011301(R)(2001).
- [5] Yu. Ts. Oganessian et al., *Phys. Rev. C*, **69**, 054607 (2004).
- [6] Yu. Ts. Oganessian et al., *Phys. Rev. Lett.* **104**, 142502 (2010).
- [7] Yu. Ts. Oganessian et al., *Phys. Rev. C* **74**, 044602 (2006).
- [8] Yu. Ts. Oganessian et al., *Phys. Rev. C* **79**, 024603 (2009).
- [9] Yu. Ts. Oganessian et al., *Phys. Rev. Lett.*, **104**, 142502 (2010).
- [10] Yu. Ts. Oganessian et al., *Phys. Rev. C* **83**, 054315 (2011).
- [11] Yu. Ts. Oganessian et al., *Phys. Rev. Lett.* **108**, 022502 (2012).
- [12] Ch. E. Düllmann et al., *Phys. Rev. Lett.* **104**, 252701 (2010).
- [13] L. Stavsetra et al., *Phys. Rev. Lett.* **103**, 132502 (2009).
- [14] G. Münzenberg et al., *Z. Phys. A* **333**, 163-175, (1989).
- [15] G. Münzenberg et al., *Z. Phys. A* **324**, 489-490, (1986).
- [16] G. Münzenberg et al., *Z. Phys. A* **315**, 145-158, (1984).
- [17] S. Hofmann and G. Münzenberg *Rev. Mod. Phys.*, **72**, 733-767 (2000).
- [18] S. Hofmann et al., *Z. Phys. A* **350**, 281-282, (1995).
- [19] S. Hofmann *Nuclear Physics News* 5, 28, (1995).
- [20] S. Hofmann et al., *Z. Phys. A*, **350**, 277(1995).
- [21] S. Hofmann et al., *Z. Phys. A*, **354**, 229-230, (1996).
- [22] S. Hofmann et al., *Z. Phys. A*, 14, 147 (2002).
- [23] S. Hofmann et al., *Eur. Phys. J. A*, **32**, 251 (2007).
- [24] G. Audi et al., *Nucl. Phys. A* 729 (2003) 1.
- [25] G. Audi, A.H. Wapstra, and C. Thibault (2003) *Nucl. Phys. A* 729, 337.
- [26] S. Goriely, M. Samyn, and J.M. Pearson, (2007) *Phys. Rev. C* 75, 064312.
- [27] P. Möller, J.R. Nix, W.D. Myers and W.J. Świątecki, *At. Data Nucl. Data Tables* **59** (1995) 185.
- [28] J. Duflo and A.P. Zuker (1995) *Phys. Rev. C* 52, 23.
- [29] J. Duflo and A.P. Zuker (1996) at <http://csn-srv3.in2p3.fr/AMDC/theory>.
- [30] P. Reiter et al., *Phys. Rev. Lett.* **82**, 509512 (1999).
- [31] S. Ćwiok et al., *Nucl. Phys. A* **420**, 254 (1983).
- [32] G. Leander et al., *Proc Int. Conf. AMCO 7-1984*, O. Klepper (ed.) TH-Darmstad p.466.
- [33] K. Boning, Z. Patyk, A. Sobiczewski, S. Ćwiok, *Z. Phys. A* **325**, 479 (1986).
- [34] A. Sobiczewski, Z. Patyk, S. Ćwiok *Z. Phys. A* **186**, 6 (1987).

- [35] S. wiok, J. Dobaczewski, P.-H. Heenen, P. Magierski and W. Nazarewicz, *Nucl. Phys. A* **611**, 211 (1996).
- [36] S. wiok, P.-H. Heenen, W. Nazarewicz, *Nature* **433**, 709 (2005).
- [37] A. Baran, Z. Lojewski, K. Sieja, and M. Kowal, *Phys. Rev. C* **72**, 044310 (2005).
- [38] K. Siwek-Wilczynska, T. Cap, M. Kowal, A. Sobiczewski, and J. Wilczyński, *Phys. Rev. C*, submitted (2012).
- [39] K. Blaum, *Physics Reports*, 425 (2006) 1.
- [40] D. Lunney, J.M. Pearson, C. Thibault, *Rev. Mod. Phys.* **75** (2003) 1021.
- [41] H.J. Krappe, J.R. Nix and A.J. Sierk, *Phys. Rev. C* **20** (1979) 992.
- [42] I. Muntian, Z. Patyk and A. Sobiczewski, *Acta Phys. Pol. B* **32**, 691 (2001).
- [43] P. Mller and J.R. Nix, *Nucl. Phys. A* **361** (1981) 117; *At. Data Nucl. Data Tables* **26** (1981) 165.
- [44] V.M. Strutinsky *Nucl. Phys. A* **95** (1967) 420.
- [45] V.M. Strutinsky *Nucl. Phys. A* **122** (1968) 1.
- [46] D. G. Madlannd and J. R. Nix, *Nucl. Phys A*, 476, 1, (1998).
- [47] S. wiok, J. Dudek, W. Nazarewicz, J. Skalski and T. Werner, *Comput. Phys. Commun.* **46** (1987) 379.
- [48] J. Bardeen, L.N. Cooper and J.R. Schrieffer, *Phys. Rev.* **108** (1957) 1175.
- [49] R. W Hasse, W. D. Myers, "Geometrical Relationships of Macroscopic Nucler Physics." *Springer-Verlag Berlin Heidelberg*, (1988).
- [50] P. Mller, R. Bengtsson, B. G. Carlsson, P. Olivius, and T. Ichikawa, *Phys. Rev. Lett.* **97**, 162502 (2006).
- [51] P. Jachimowicz, M. Kowal, P. Rozmej, J. Skalski and A. Sobiczewski, *Int. J. Mod. Phys. E* **18**, **4**, 1088 (2009).
- [52] P. Jachimowicz, M. Kowal, P. Rozmej, J. Skalski and A. Sobiczewski, *Int. J. Mod. Phys. E* **19**, **4**, 768 (2010).
- [53] P. Jachimowicz, M. Kowal, P. Rozmej, J. Skalski and A. Sobiczewski, *Int. J. Mod. Phys. E* **20**, **2**, 514 (2011).
- [54] P. Jachimowicz, M. Kowal, J. Skalski, *Int. J. Mod. Phys. E* **19**, 508 (2010).
- [55] R. E. Bellman, R. E. Kalaba, "Quasilinearization and nonlinear boundary value problems", American Elsevire, New York, (1965).
- [56] A. Baran, K. Pomorski, A. Lukasiak and A. Sobiczewski, *Nucl. Phys. A* **361**, (1981).
- [57] S. wiok and A. Sobiczewski, *Z. Phys. A* **342**, (1992).
- [58] R. A. Gherghescu, J. Skalski, Z. Patyk and A. Sobiczewski, *Nucl. Phys. A* **651**, (1999).
- [59] V. Luc and P. Soille, *IEEE Trans. Pattern Anal. Mach. Intell.*, **13**, 583 (1991).
- [60] A. Mamdough, J.M. Pearson, M. Rayet, and F. Tondeur, *Nucl. Phys. A* **644**, 389 (1998).
- [61] B. Hayes, *Am. Sci.* **88**, 481 (2000).
- [62] P. Mller, A. J. Sierk and A. Iwamoto, *Phys. Rev. Lett.* **92**, 072501 (2004).
- [63] P. Mller, A. J. Sierk, T. Ichikawa, A. Iwamoto, R. Bengtsson, H. Uhrenholt, and S. berg, *Phys. Rev. C* **79**, 064304 (2009).
- [64] R. Capote et. al. Nuclear Data Sheets 110 (2009) 31073214, <http://www-nds.iaea.org/RIPL-3/>.
- [65] P. Jachimowicz, M. Kowal, J. Skalski, *Phys. Rev. C* **83**, 054302, (2011).
- [66] M. Kowal, P. Jachimowicz, A. Sobiczewski, *Phys. Rev. C* **82**, 014303, (2010).
- [67] A. Dobrowolski, K. Pomorski, and J. Bartel, *Phys. Rev. C* **75**, 024613 (2007).
- [68] H. Abusara, A. V. Afanasjev, and P. Ring *Phys. Rev. C* **82**, 044303, (2010).
- [69] H. Abusara, A. V. Afanasjev, and P. Ring *Phys. Rev. C* **85**, 024314, (2012).
- [70] J. Erler, K. Langanke, H. P. Loens, G. Martnez-Pinedo, and P.-G.Reinhard *Phys. Rev. C* **85**, 025802, (2012).
- [71] R. Smolanczuk, J. Skalski and A. Sobiczewski: *Phys. Rev. C* **52**, 1871 (1995).